

SYNTHETIC GAUGE FIELDS FOR ULTRACOLD ATOMS IN SYNTHETIC DIMENSIONS

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Phase transitions

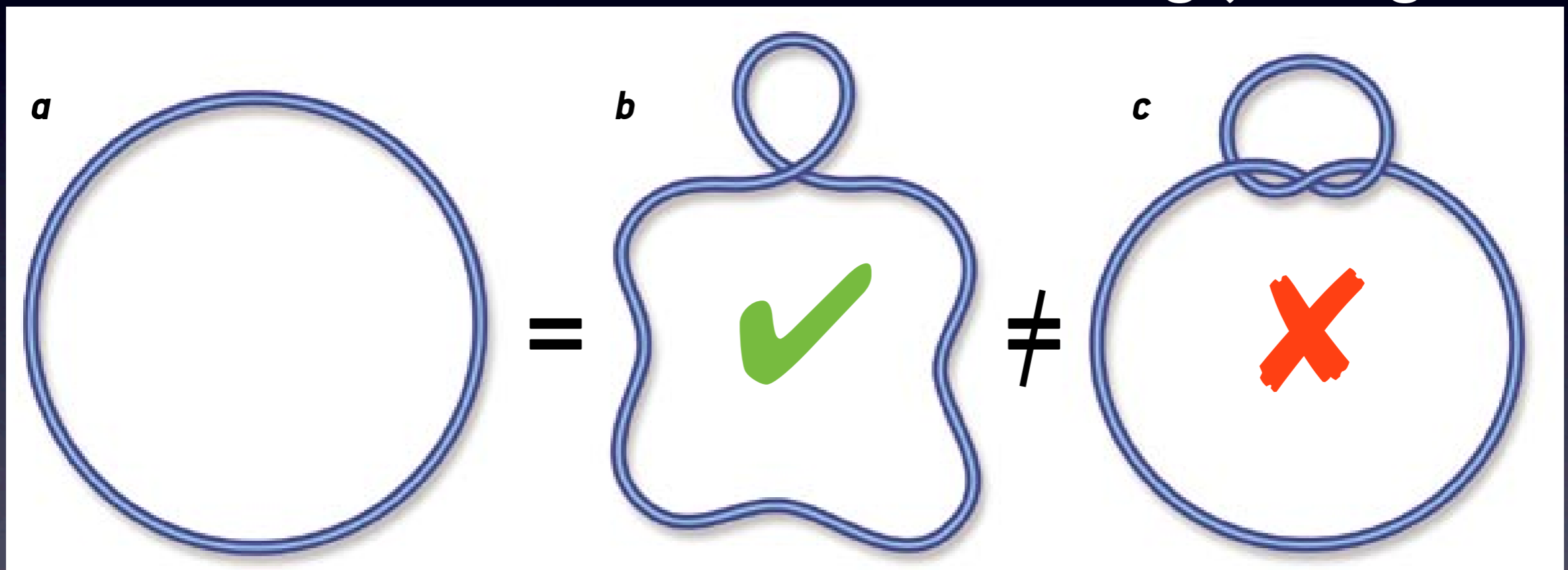
- **Landau**: most phases of matter may be classified by the symmetries they break
 - ▶ translational (solids)
 - ▶ rotational (magnets)
 - ▶ gauge (superfluids)
- **BUT**: some materials possess distinguishable phases without breaking symmetries
(QH and QSH effect)

Topological phase transitions!

Topological properties

✓: stretching, bending

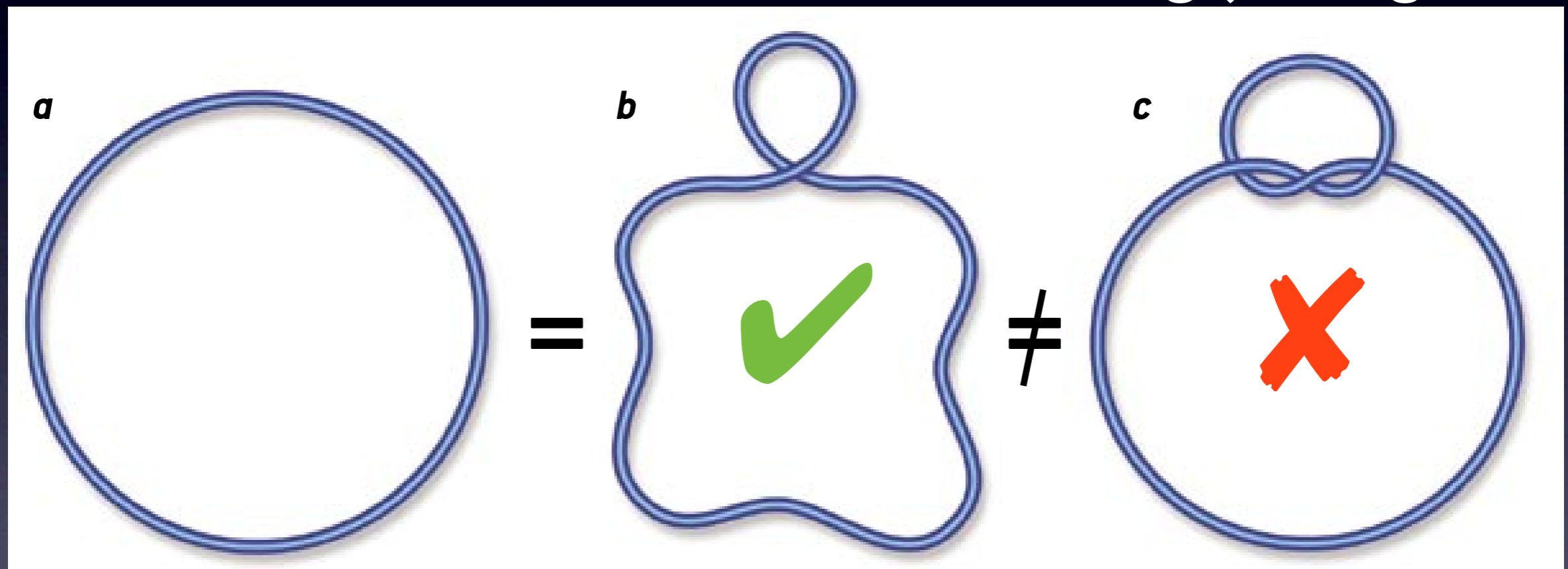
✗: cutting, joining



Topological properties

✓: stretching, bending

✗: cutting, joining



Concern the whole system (non-local)

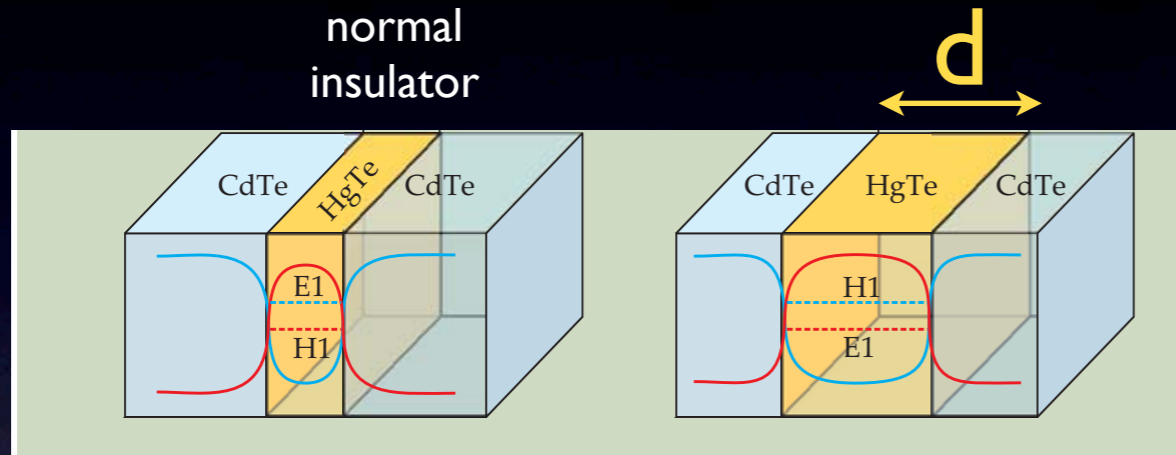
Characterized by integer numbers

Robust

A topological insulator

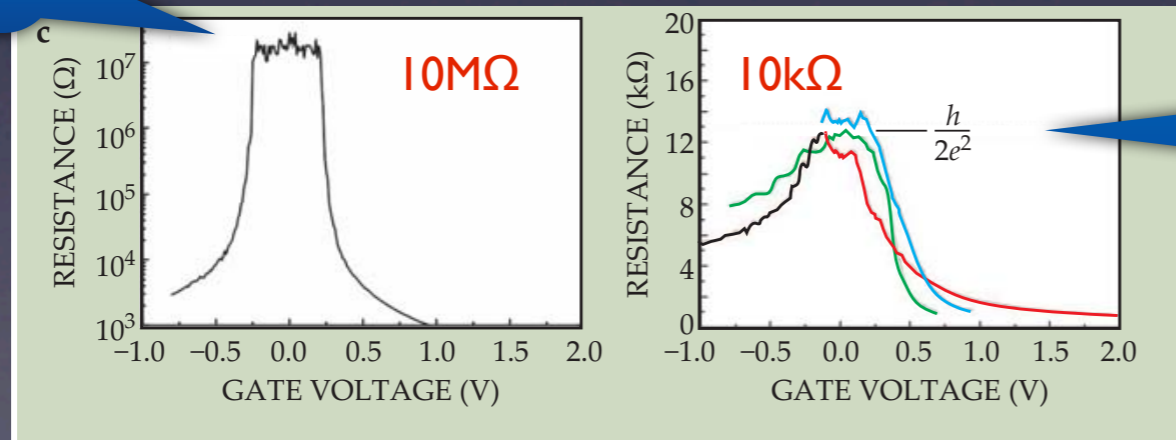
Hg-Te quantum well

Hg: Mercury
Te: Telluride



Phase transition at $d=d_{\text{crit}}$:
normal-to-topological insulator

very large
resistance



independent of d , when $d > d_{\text{crit}}$
2 quanta of conductance

Qi & Zhang, Physics Today 2010

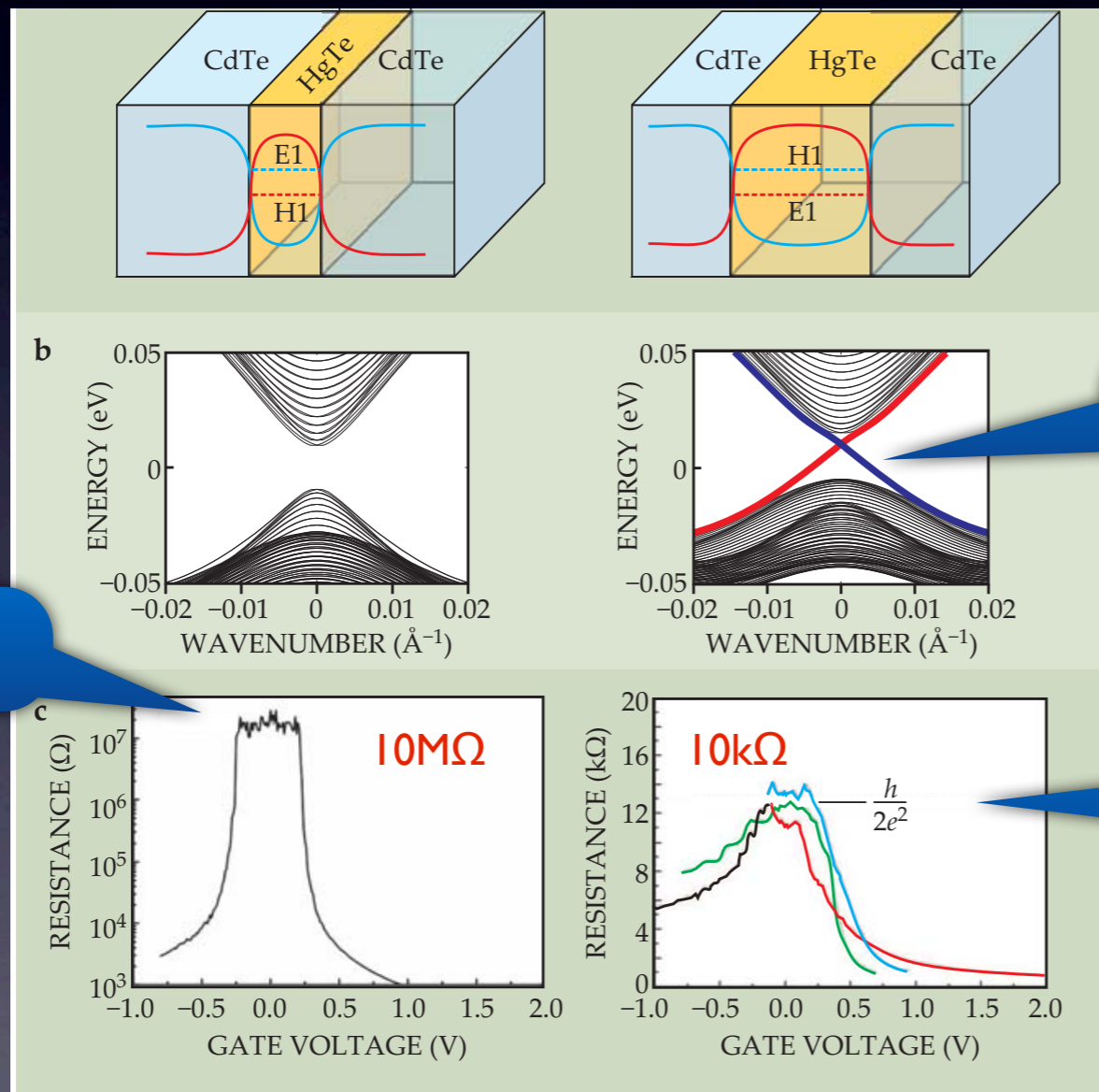
A topological insulator

Hg-Te quantum well

Hg: Mercury
Te: Telluride

normal
insulator

d



$d > d_{\text{crit}}$: topological insulator

edge states

Hg-Te has strong
spin-orbit coupling

very large
resistance

2 quanta of conductance
(independent of d , when $d > d_{\text{crit}}$)

Qi & Zhang, Physics Today 2010

interesting..., but where?

- exotic condensed matter systems
(quantum wells, bismuth antimony alloys, Bi_2Se_3 crystals, ...)
- $\nu=5/2$ FQH state (Pfaffian)
- ultracold atoms?

Outlook of the talk

Synthetic gauge fields

$\uparrow\downarrow$ 2D s-wave fermionic SF
with $n_{\uparrow} \neq n_{\downarrow}$
and spin-orbit coupling

Synthetic dimensions

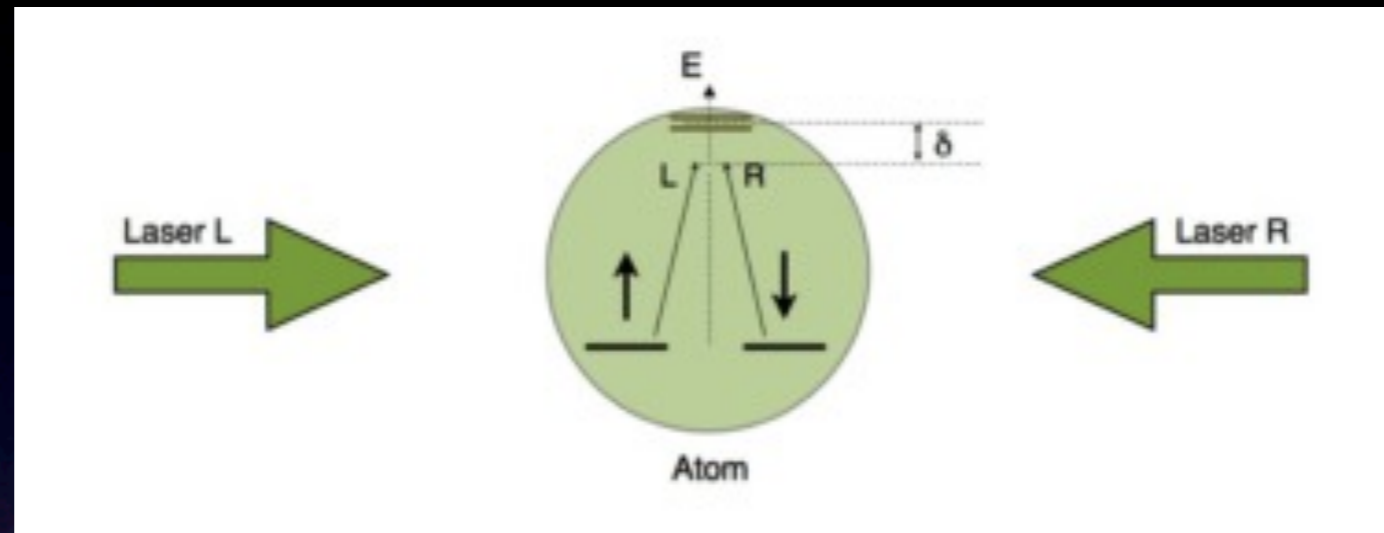
Synthetic gauge fields for neutral atoms

Theory: Jaksch&Zoller, NJP 2003
Osterloh et al., PRL 2005
Gerbier&Dalibard, NJP 2010
Bermudez et al., PRL 2010 (TRI Top. Ins.)

- adiabatic Raman passage
- adiabatic control of superpositions of degenerate dark states
- spatially varying Raman coupling
- Raman-induced transitions to auxiliary states in optical lattices

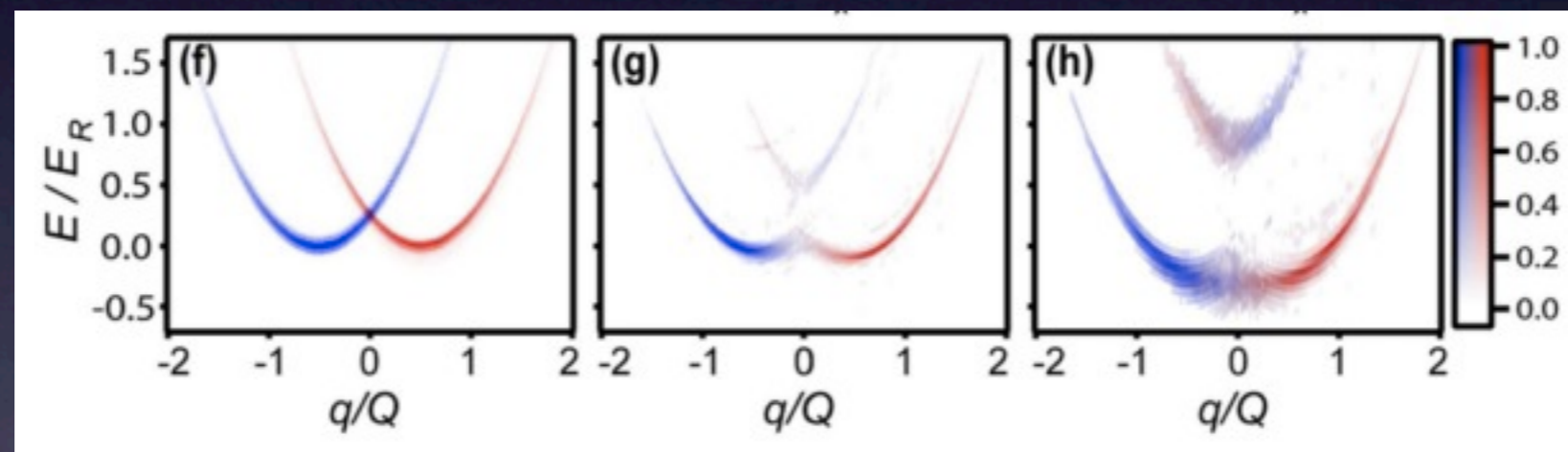
REVIEW: *Artificial gauge potentials for neutral atoms*
J. Dalibard, F. Gerbier, G. Juzeliūnas, and P. Öhberg, RMP 2011

Synthetic gauge fields for neutral atoms



$$|\uparrow, q=k_x - Q/2\rangle$$

$$|\downarrow, q=k_x + Q/2\rangle$$



spin-orbit gap

increasing intensity of Raman lasers

spin flip \leftrightarrow momentum kick,
i.e., spin-orbit coupling

P.Wang et al., PRL 2012 (Shanxi U.)
L.W. Cheuk et al., PRL 2012 (MIT)

a field moving fast..

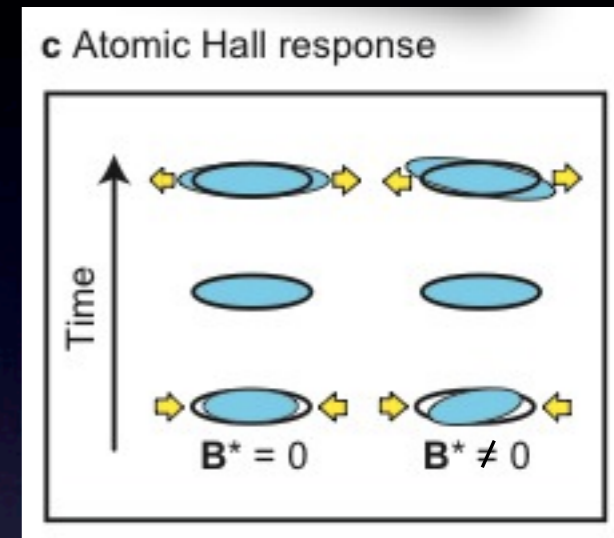
NIST: *Synthetic magnetic fields for ultracold neutral atoms*, Nature (2009)

A synthetic electric force acting on neutral atoms, Nature Phys. (2011)

Spin-orbit-coupled Bose-Einstein condensates, Nature (2011)

Observation of a superfluid Hall effect, PNAS (2012)

Peierls Substitution in an Engineered Lattice Potential, PRL (2012)



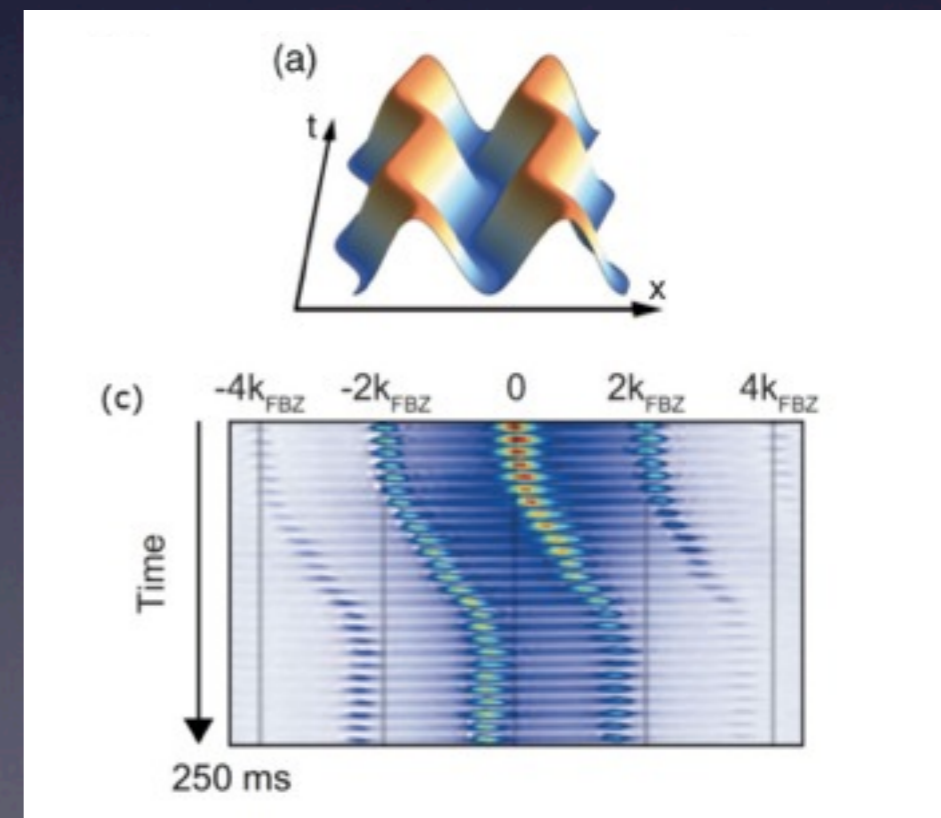
ICFO & Hamburg & Dresden:

Tunable Gauge Potential for Neutral Spinless Particles in Driven Optical Lattices, PRL (2012)

(method independent of the internal structure of the atoms!!)

Munich: *Experimental realization of strong effective magnetic fields in an optical lattice*, PRL (2011)

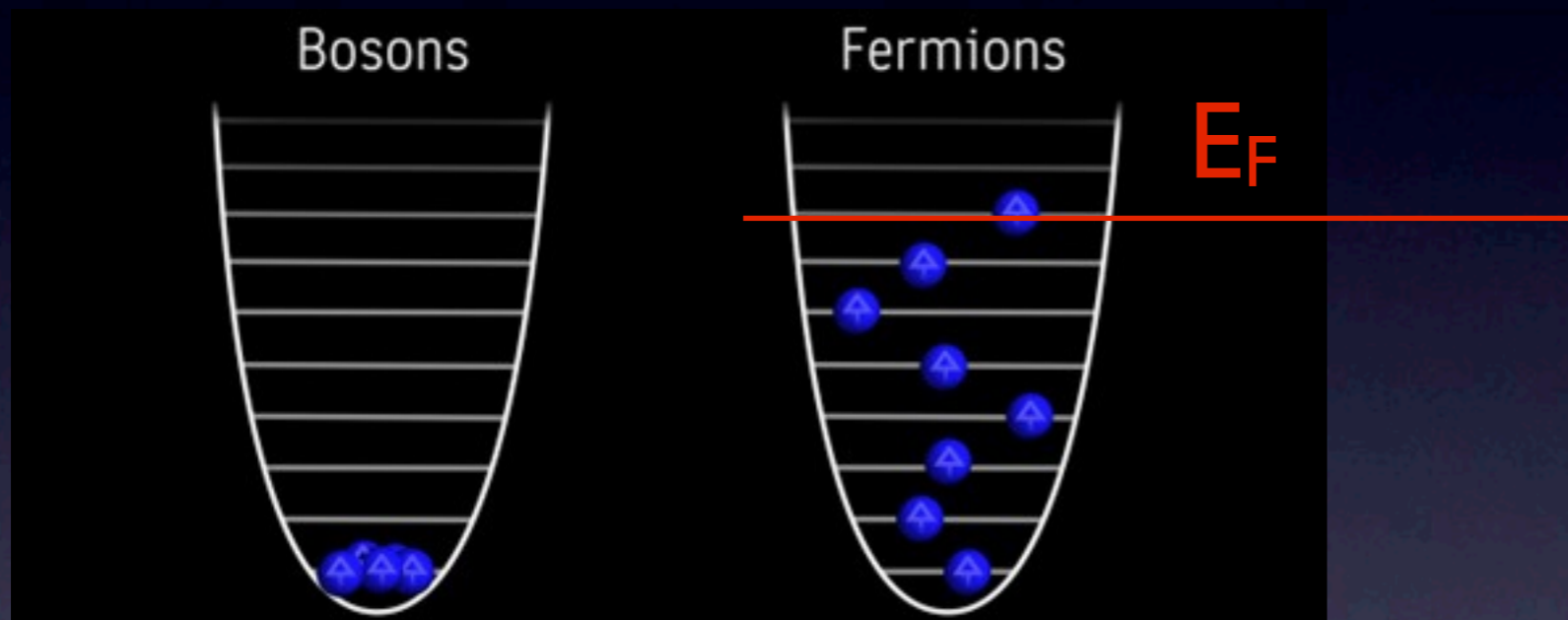
.....



\uparrow - \downarrow fermionic SF
with $n_{\uparrow} \neq n_{\downarrow}$
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Fermions vs. Bosons

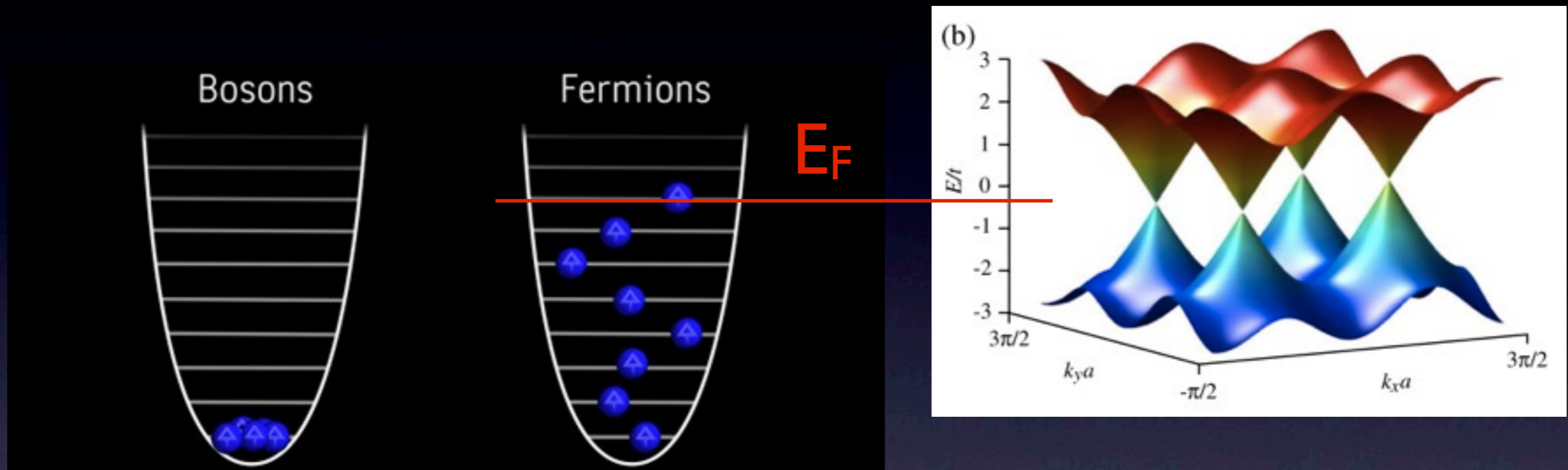
Bosons condense in the lowest available energy state.



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Fermions vs. Bosons

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On the contrary, fermions have to due to obey the Pauli principle.

By changing the number of particles, we are able to investigate the interesting excitations: the system becomes sensitive to the topological properties of the band structure.

$\uparrow\downarrow$ fermions in synthetic gauge fields

$$\mathbf{c}_i^\dagger = (c_{i\uparrow}^\dagger, c_{i\downarrow}^\dagger)$$

$$\mathcal{H}_0 = -t \sum_i \left[c_{i+\hat{x}}^\dagger e^{i\sigma_y \alpha} c_i + c_{i+\hat{y}}^\dagger e^{i\sigma_x \beta} c_i + \text{h.c.} \right]$$

complex hoppings = Peierl's phases

External non-Abelian gauge fields yield a **fictitious spin-orbit coupling**

Add attractive interactions



BCS superfluid



Sato, Takahashi & Fujimoto, PRL 2009

Sau Jay, Lutchyn, Tewari and Das Sarma, PRL 2010

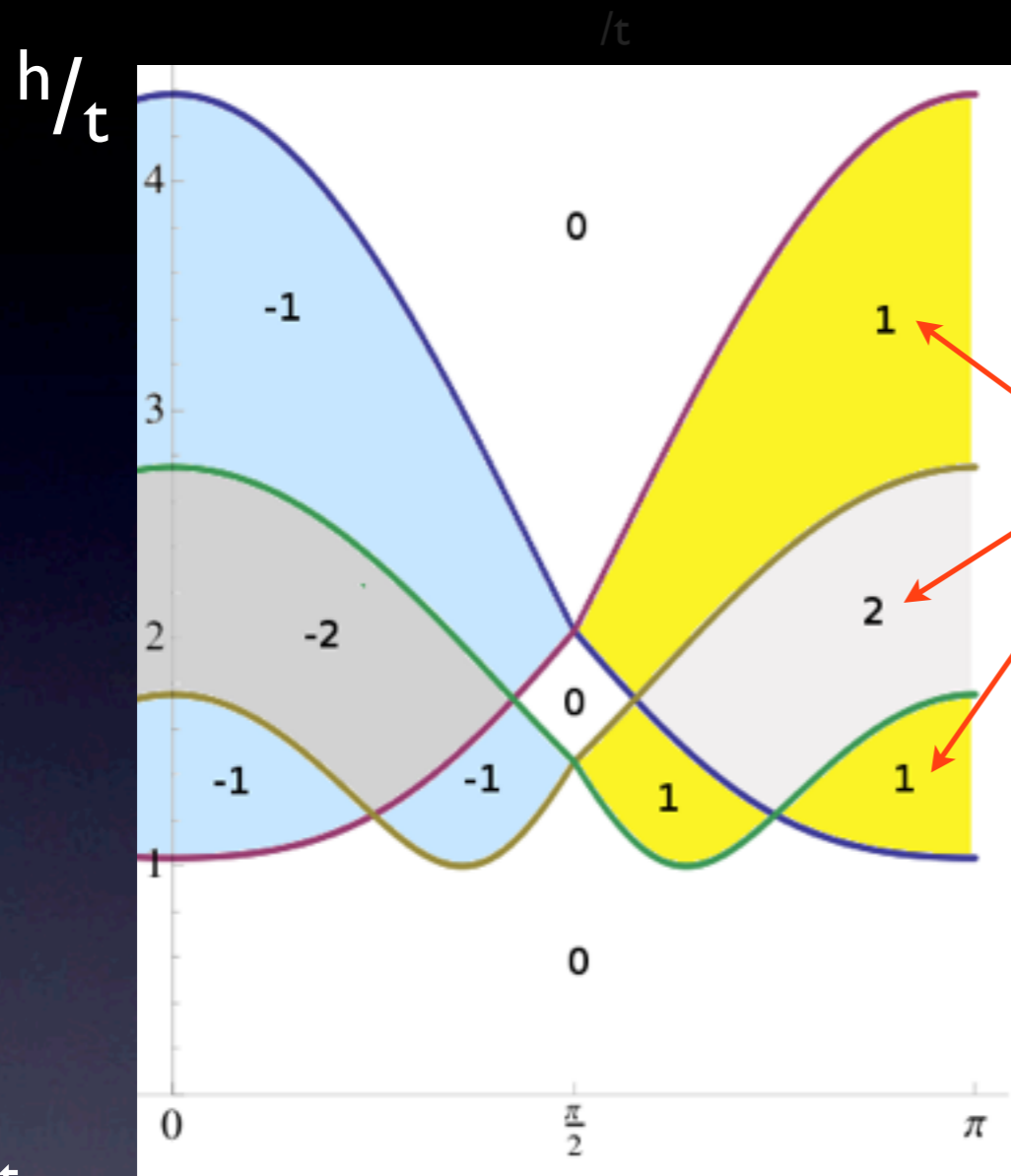
strong imbalance \Rightarrow topological states

Time-reversal and spin-rotation invariances are destroyed by the Zeeman and SO terms as a consequence our BCS Hamiltonian belongs to the most general symmetry class “D”

(Altland&Zirnbauer, PRB 1997)

its topological phases are indexed in terms of an integer number

Topological phases



$$h = \mu_{\uparrow} - \mu_{\downarrow}$$

Chern numbers

easy to calculate!

(see J. Bellissard, condmat/9504030)

Gap closing at $(\mathbf{k}_0, \tilde{h})$:

$$\mathcal{H}_{\text{eff}}(\mathbf{k}, h) = E(\mathbf{k}, h) + \vec{\sigma} \cdot \vec{f}(\mathbf{k}, h)$$

$$\Delta \text{CN}(\tilde{h}) = \text{sign}\{\det[J_{\vec{f}}(\mathbf{k}_0, \tilde{h})]\}.$$

β

$$\Delta = t$$

$$\alpha = \pi/4$$

$$\mu = -0.5t[|\cos(\alpha)| + |\cos(\beta)|]$$

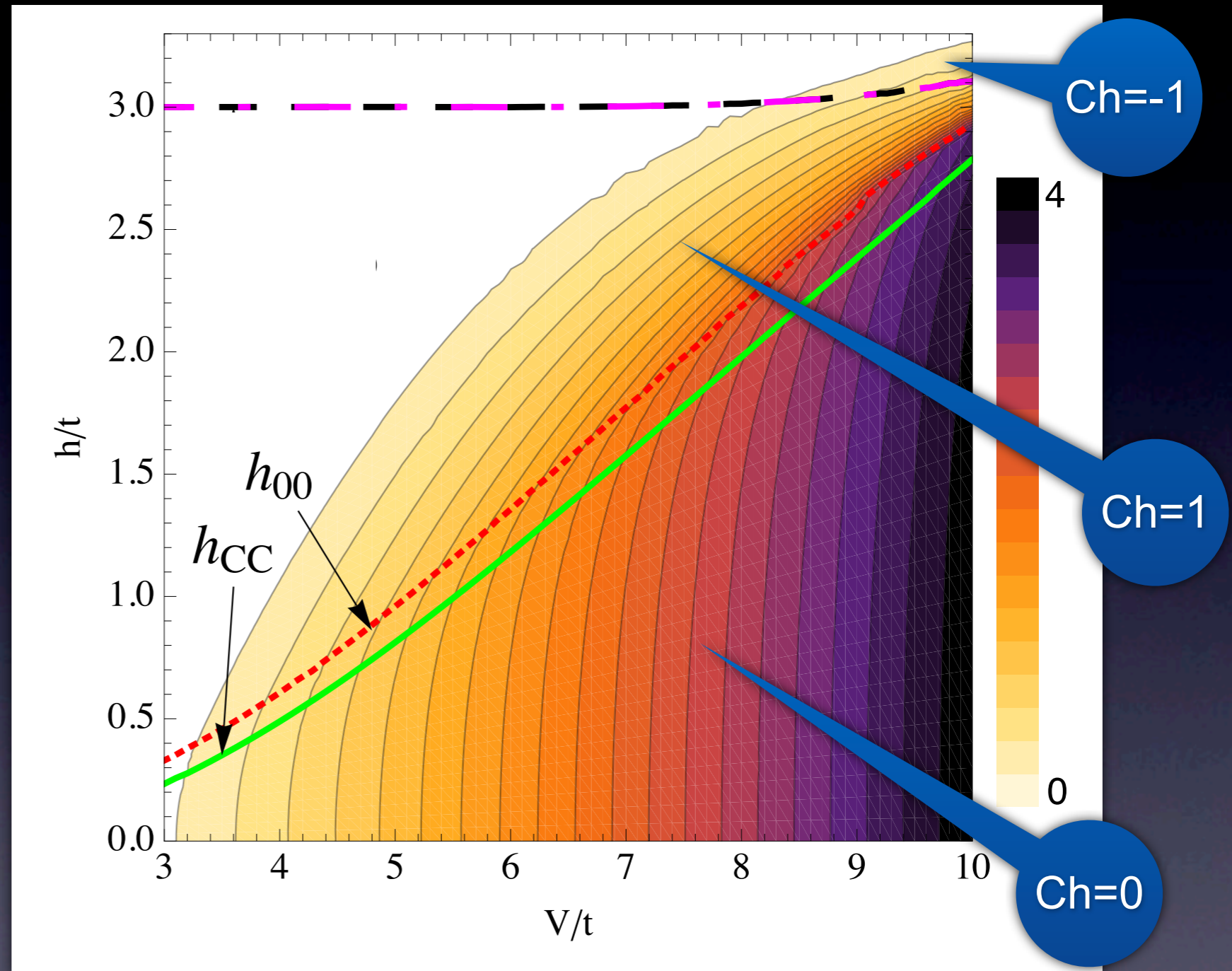
A. Kubasiak, P.M. & M. Lewenstein, EPL 2010

Spin imbalance vs. pair breaking

without SO coupling:
analytic CC limit
($h_{CC} = \Delta_0/\sqrt{2}$)

with SO coupling:
self-consistent calculation of Δ
from the BCS gap equation

$$\alpha = \beta = \pi/4 \quad \mu = -3t$$



A. Kubasiak, PM & M. Lewenstein, EPL 2010

Synthetic dimensions

Q. Sim. & Extra Dimensions

Quantum simulation with ultracold atoms:

- Hubbard model (SF-MI transition, ...)
- synthetic gauge fields (relativistic dispersions, ...)
- strongly-correlated states (QH, spin liquids, ...)

Extra (=non-spatial) dimensions:

- attempts to unify gravitation with electro-weak forces (Kaluza-Klein, Yang-Mills, ...)
- thermal QFT: compactification of euclidean time leads to Matsubara frequencies

(extra-dim is usually discrete and compact)

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quantum simulation of an extra dimension?

The main idea

- use a system with D spatial dimensions
- encode the $(D+1)^{\text{th}}$ dimension in a different degree of freedom (e.g., the spin)

$$H = -J \sum_{d=1}^{D+1} \sum_{\tilde{\mathbf{r}}} \hat{a}_{\tilde{\mathbf{r}}+\mathbf{u}_d}^\dagger \hat{a}_{\tilde{\mathbf{r}}} + \text{h.c.} \quad \tilde{\mathbf{r}} = (\mathbf{r}, \sigma)$$

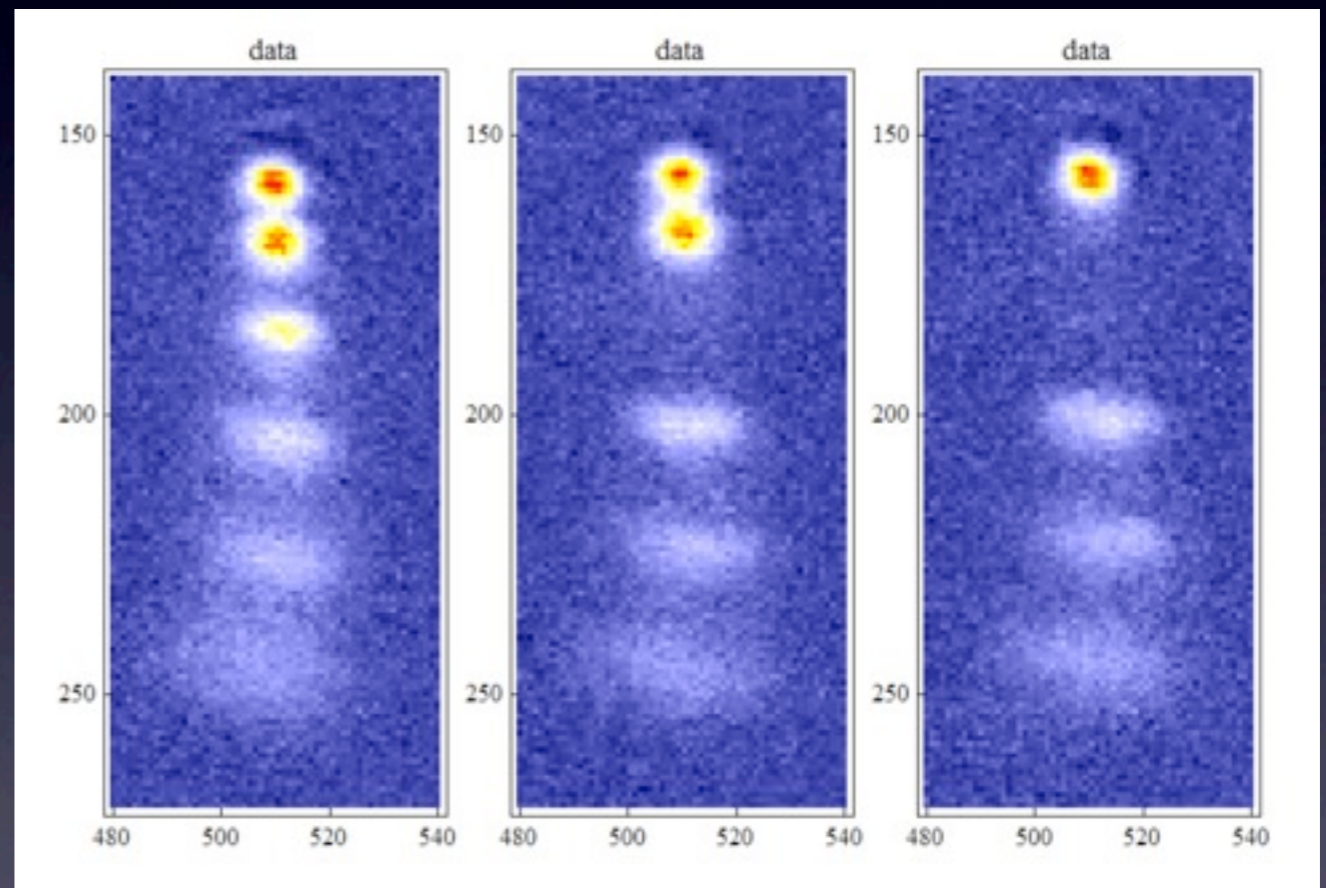
$$= -J \sum_{\sigma=1}^N \left[\sum_{d=1}^D \sum_{\mathbf{r}} \hat{a}_{\mathbf{r}+\mathbf{u}_d}^{(\sigma)\dagger} \hat{a}_{\mathbf{r}}^{(\sigma)} + \hat{a}_{\mathbf{r}}^{(\sigma+1)\dagger} \hat{a}_{\mathbf{r}}^{(\sigma)} \right] + \text{h.c.}$$

important: allow only nearest-neighbor “spin-tunneling”

Large N systems

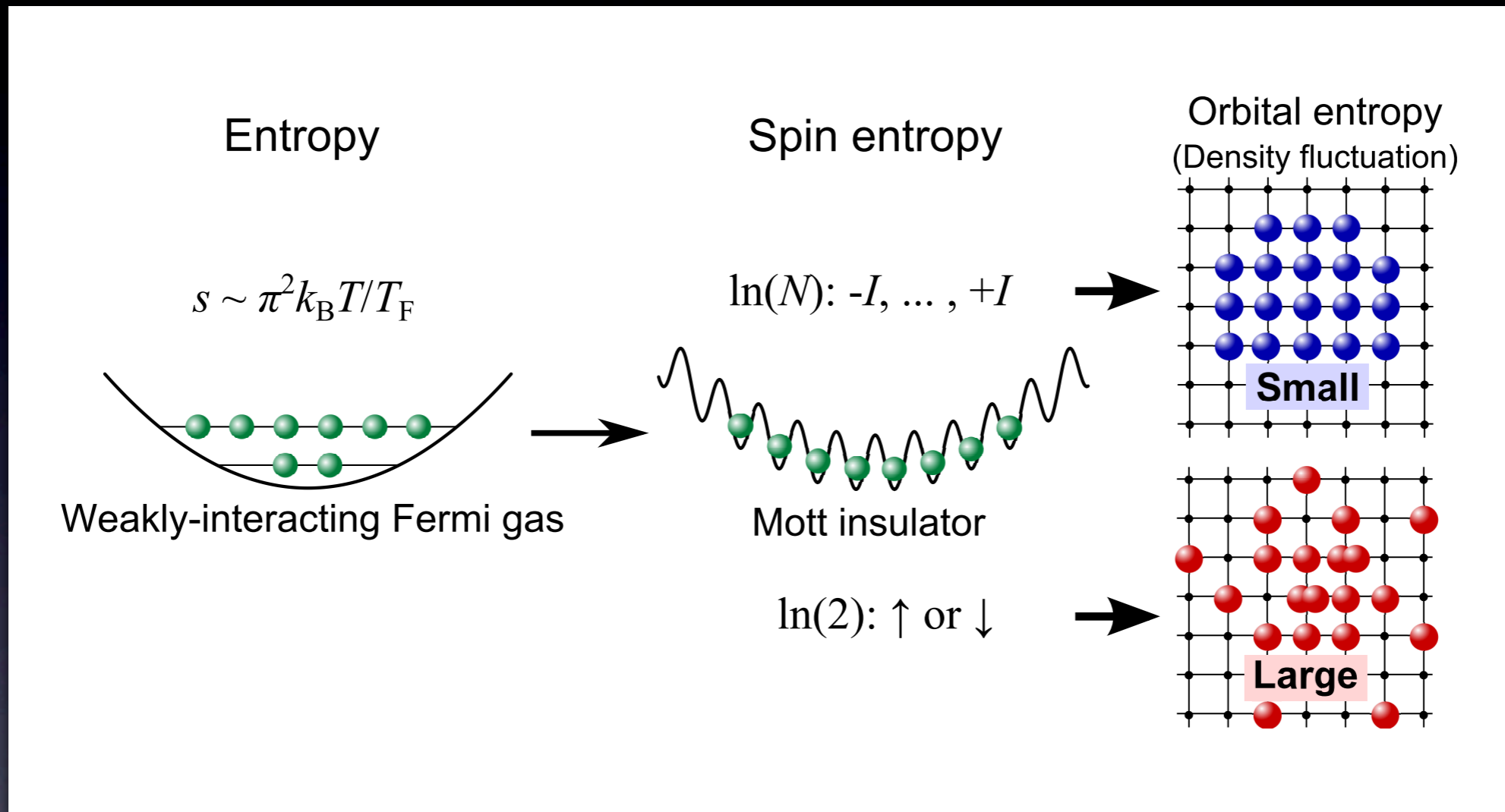
species	N
Li	2,3,...
^{87}Rb	3
^{173}Yb	6
^{40}K	2,...,10
^{87}Sr	10
^{165}Ho	120

^{173}Yb at LENS:



interactions in earth-alkali atoms are $\text{SU}(N)$ invariant!

SU(6) Mott insulator

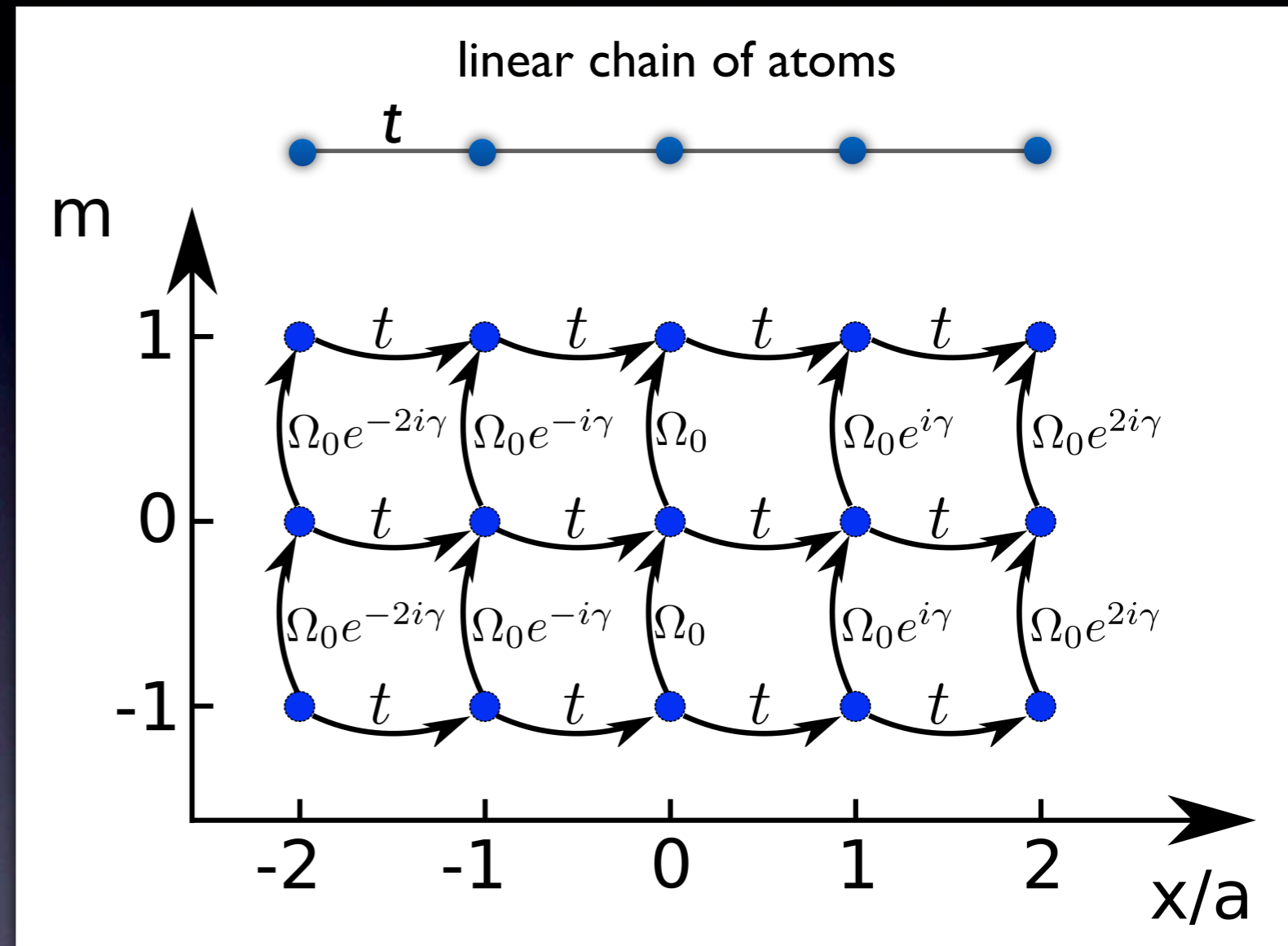
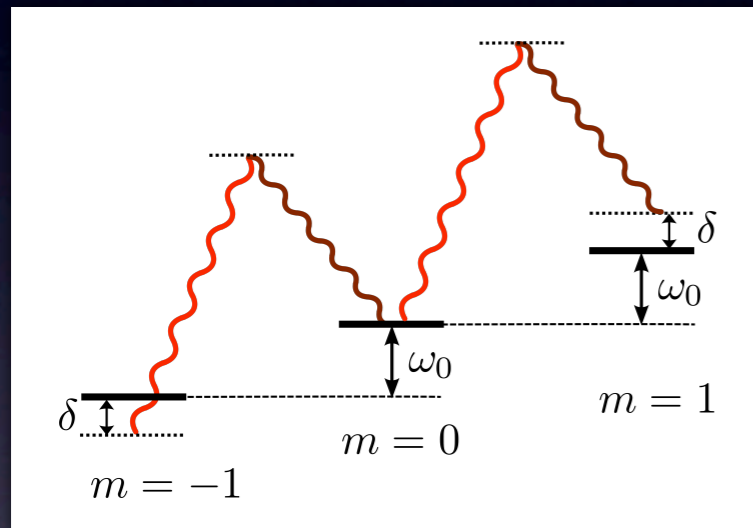


S.Taie, R.Yamazaki, S.Sugawa, and Y.Takahashi, Nature Phys. 2012

Novel cooling mechanisms?

Implementation

laser-assisted
spin-tunneling



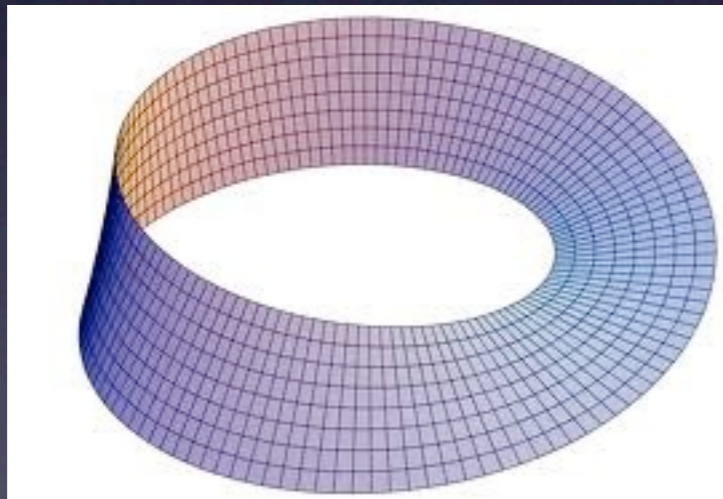
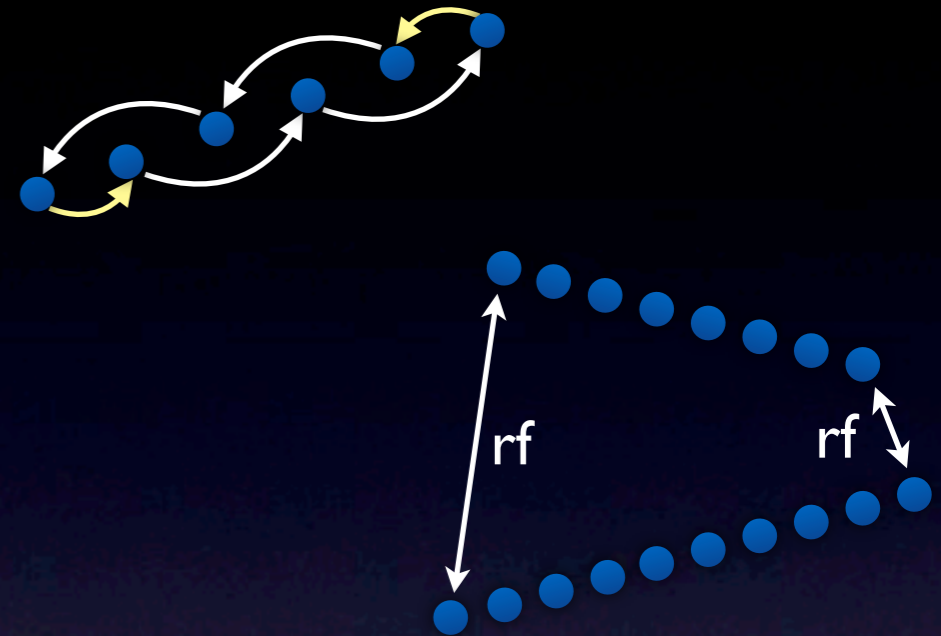
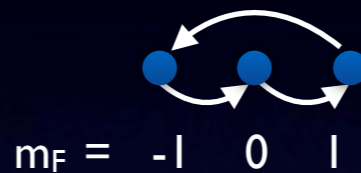
yields strong and non-staggered magnetic fluxes
and long-ranged interactions

PM, A. Celi, I. Spielman, G. Juzeliunas, and M. Lewenstein, in preparation

Interesting topologies

possible boundary conditions along the spin direction:

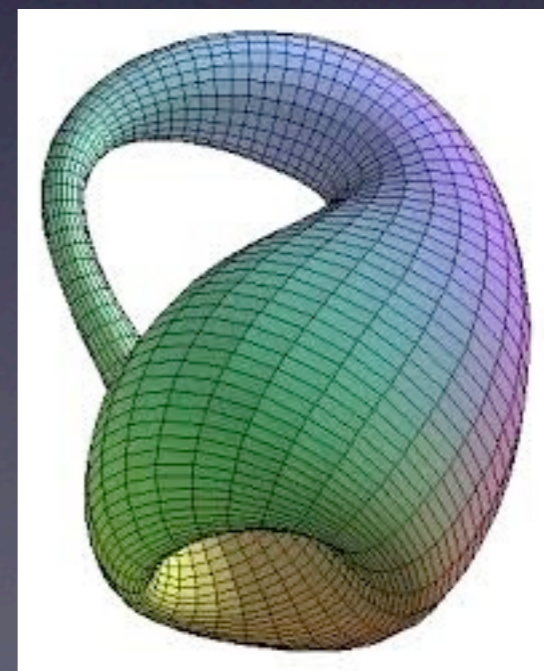
- open
- closed
- twisted (a closed loop encircles a phase)



Möbius strip
linear chain in the spatial dir.,
 $\pi/2$ twist in spin

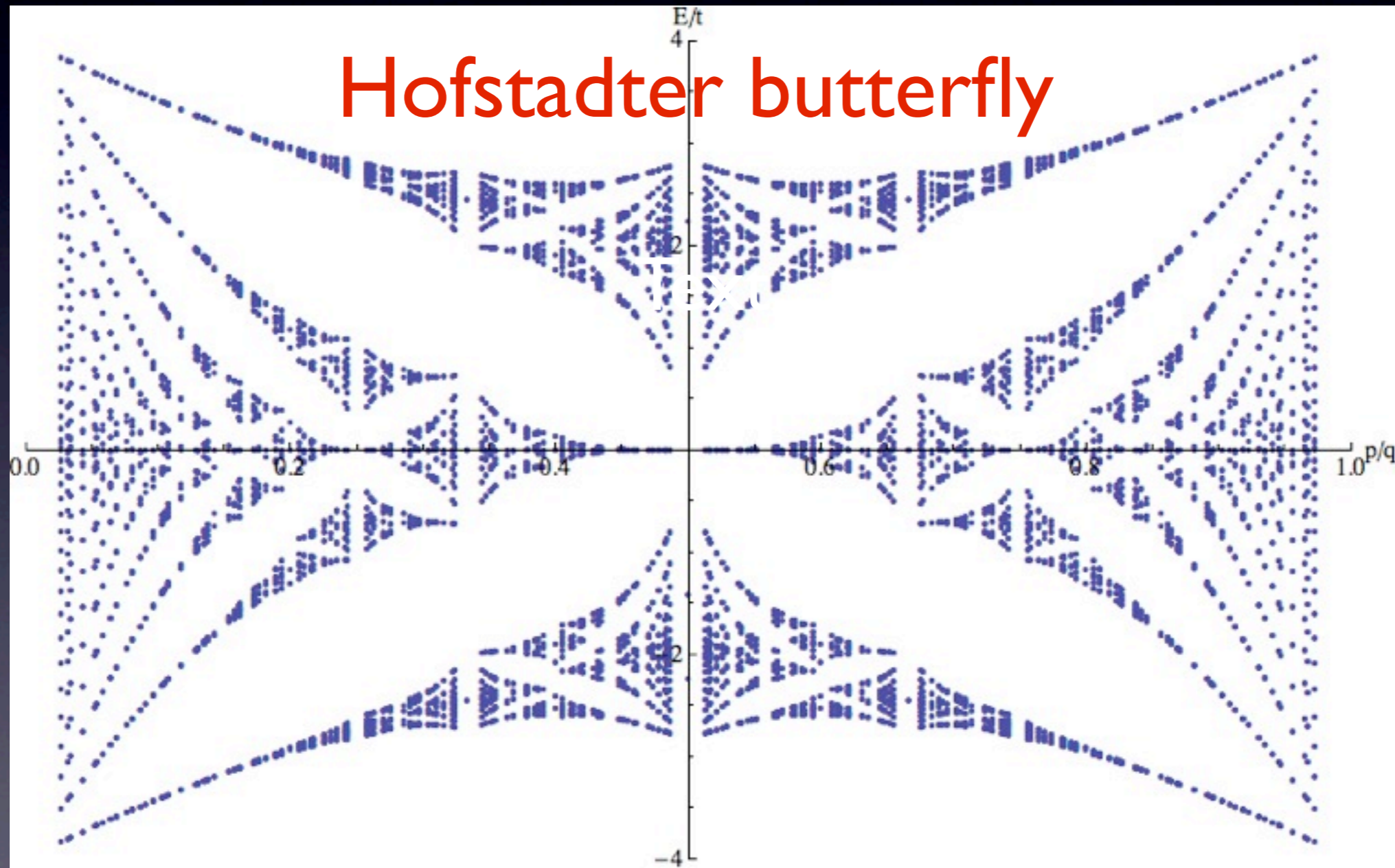
Klein bottle

ring in the spatial dir.,
 $\pi/2$ twist in spin



Energy spectrum of spin-1 atoms with closed b.c. and non-zero flux

$$\Phi = 2\pi(p/q)$$



in collaboration with



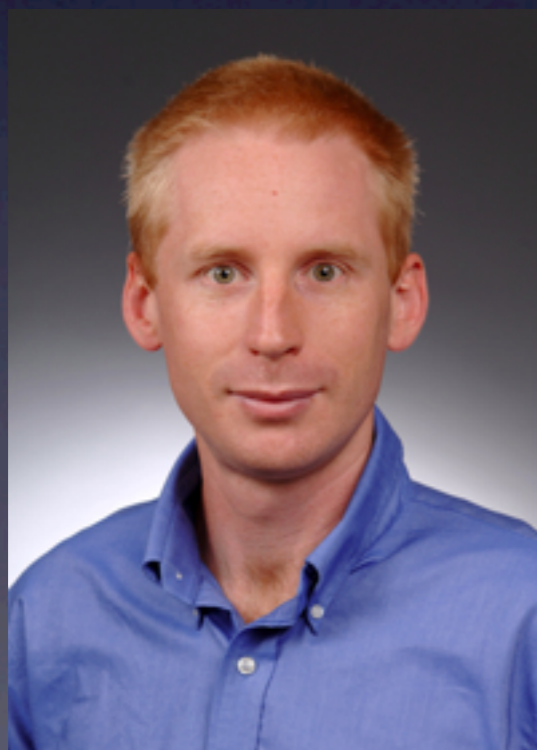
Maciej Lewenstein



Alessio Celi



Gediminas Juzeliunas



Ian Spielman



Anna Kubasiak



Anna Sanpera

Conclusions

- Gauge fields yield non-trivial topological phases
- Superfluidity in $\uparrow\downarrow$ fermions is stabilized by a non-Abelian gauge field
- Using an internal d.o.f. as an extra-dimension:
 - ★ quantum simulation of high-energy theories, and $D>3$ systems (e.g., crit. exp. of ph. trans.)
 - ★ novel cooling schemes possible?

PM, A. Sanpera & M. Lewenstein, PRA(R) 2010

A. Kubasiak, PM & M. Lewenstein, EPL 2010

O. Boada, A. Celi, J.I. Latorre, and M. Lewenstein, PRL 2012

PM, A. Celi, I. Spielman, G. Juzeliunas, and M. Lewenstein, in preparation