

# Bose polarons at finite temperature and strong coupling

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# Outline

- ◆ Quantum mixtures
- ◆ Impurities in an ideal Fermi sea (“Fermi polarons”)
- ◆ Impurities in a weakly-interacting Bose gas (“Bose polarons”)
  - ◆ Zero-temperature physics
  - ◆ New features appearing at non-zero temperature

# Collaborators



Nils Guenther



Maciej Lewenstein



Georg M. Bruun

# Quantum Mixtures in CondMat

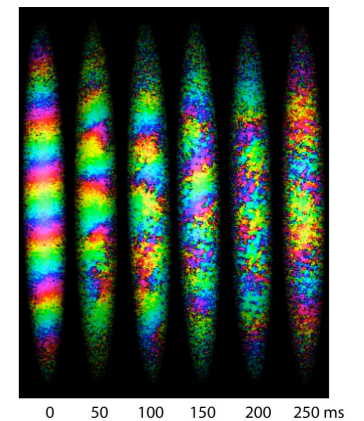
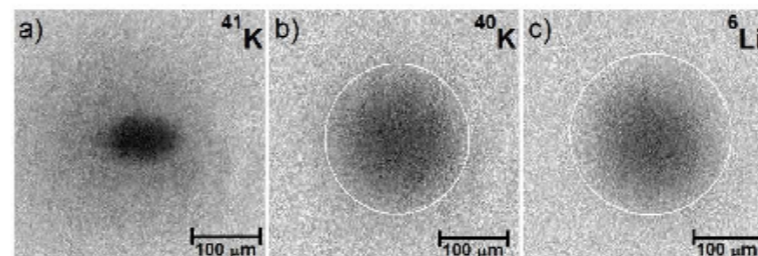
- ♦  $^3\text{He}$ - $^4\text{He}$
- ♦ ultracold gaseous mixtures:
  - ♦ FF (BEC-BCS crossover)
  - ♦ B+FF superfluids (coherent/damped dynamics)
  - ♦ BB mixtures (ultradilute quantum liquid droplets)
  - ♦ spinor gases,  $\text{SU}(N)$  invariant systems
- ♦ quantum magnets, quantum Hall systems, spin-liquids
- ♦ quark-gluon plasma
- ♦ neutron stars

[Zwerger, Lecture Notes in Phys.]

ENS-Paris

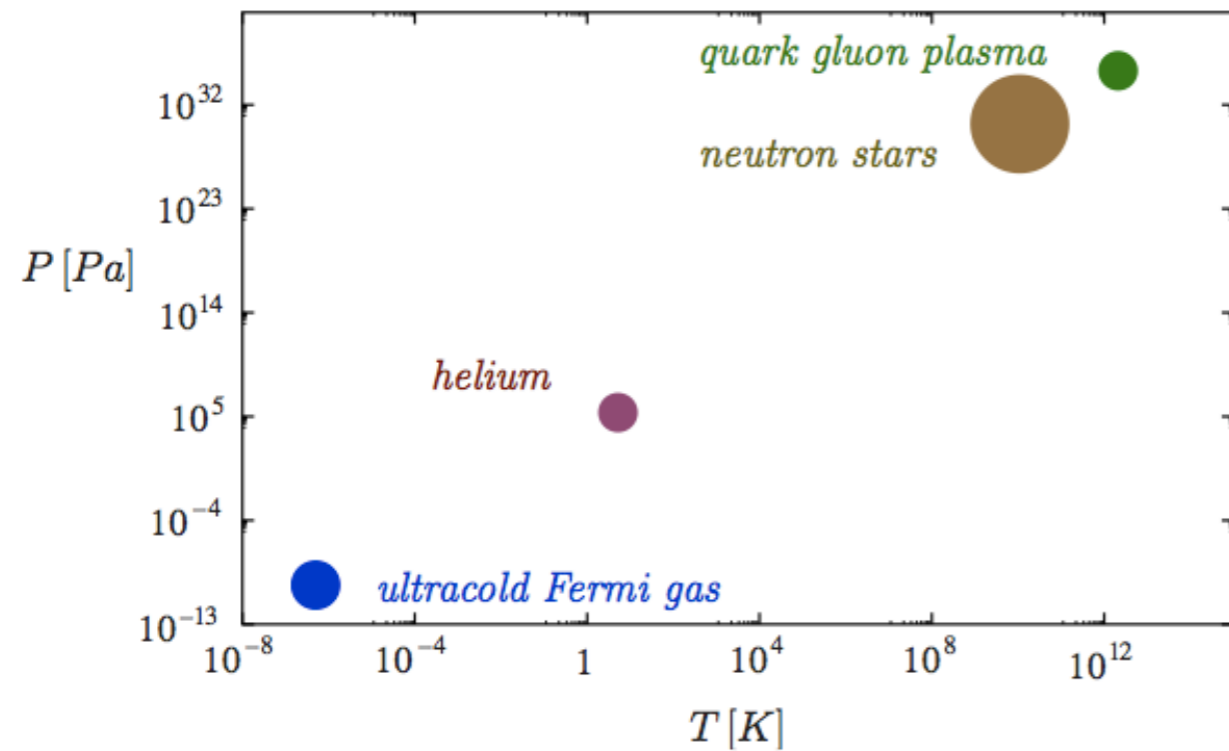
Stuttgart, Innsbruck, Barcelona

Kyoto, Florence, Munich, ...



Very different microscopically, but  
 $\exists$  common ***emergent and universal many-body descriptions.***

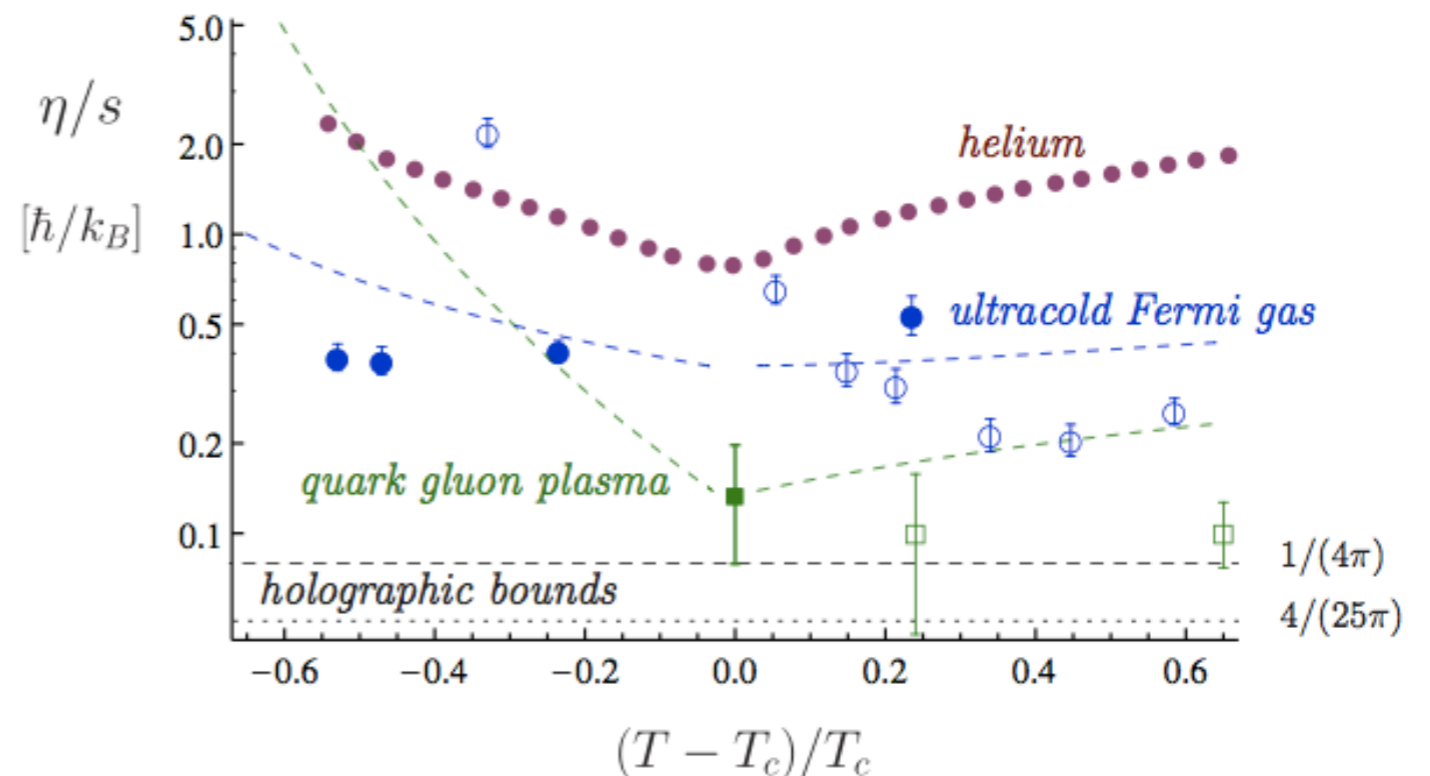
# Universality in Quantum Mixtures



20 orders of magnitude difference in temperature

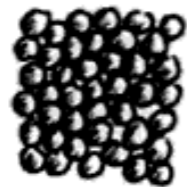
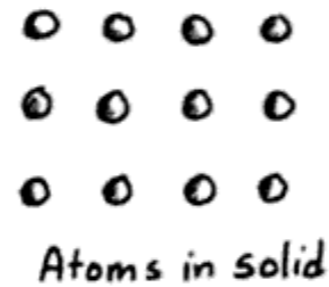
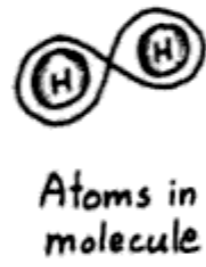
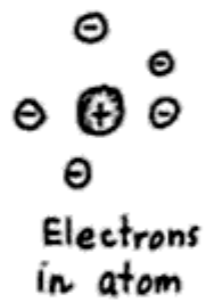
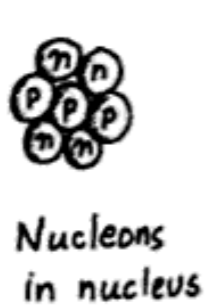
but similar transport properties!

e.g.,  
shear viscosity/entropy density:

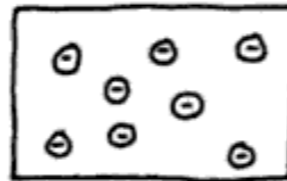


# Many-body systems

## A GUIDE TO FEYNMAN DIAGRAMS



Molecules  
in liquid



Electrons  
in metal

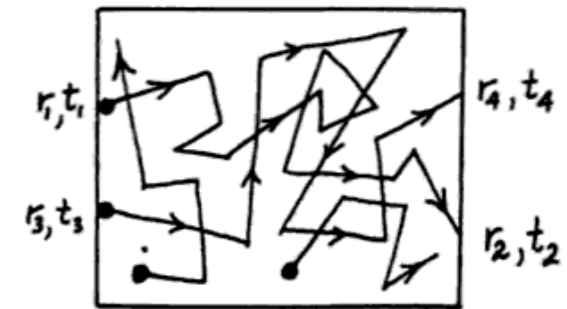
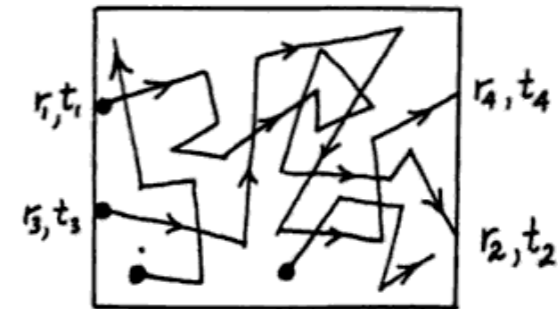


Fig. 0.1 *Some Many-body Systems*

(from Richard Mattuck's book)

# Quasi-Particles

No chance of studying **real particles**



Landau:  
of importance are the collective excitations,  
which generally behave as **quasi**-particles!

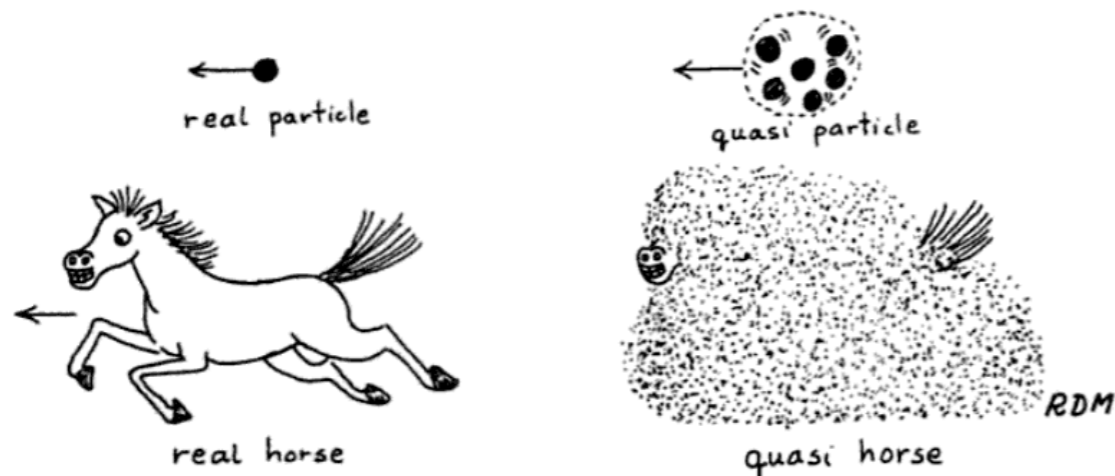
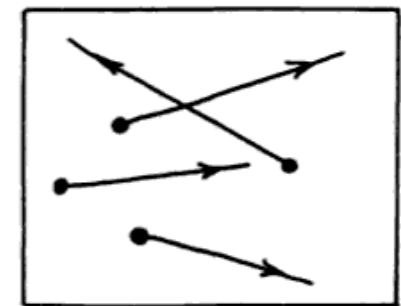


Fig. 0.4 Quasi Particle Concept

a **QP** is a “free” particle with:  
@ q. numbers (charge, spin, ...)  
@ renormalized mass  
@ chemical potential  
@ shielded interactions  
@ lifetime

# Ultracold atoms

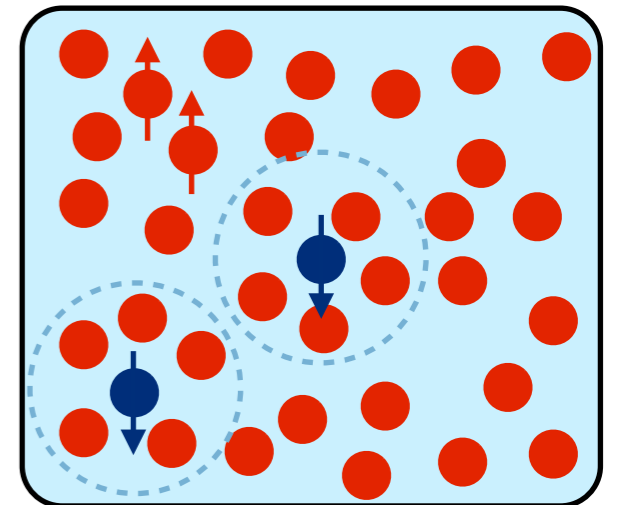


- ◆ chemical composition
- ◆ interaction strength
- ◆ temperature
  
- ◆ periodic potentials
- ◆ physical dimension
- ◆ atom-light coupling
- ◆ exotic interactions
  - (x-wave, spin-orbit)
- ◆ dynamics
- ◆ disorder
- ◆ periodic driving
  - (shaken optical lattices)



# Imbalanced Fermi gases

Two-component Fermi gas with  $N_{\uparrow} \gg N_{\downarrow}$ :  
a strongly-interacting system,  
or an ensemble of weakly-interacting quasi-particles  
(a *Fermi liquid*)



$$E = \frac{3}{5} \epsilon_F N_{\uparrow} \left[ 1 + \frac{m}{m^*} \left( \frac{N_{\downarrow}}{N_{\uparrow}} \right)^{5/3} \right] + N_{\downarrow} E_p + \dots,$$

kinetic energy  
of the **Fermi sea**

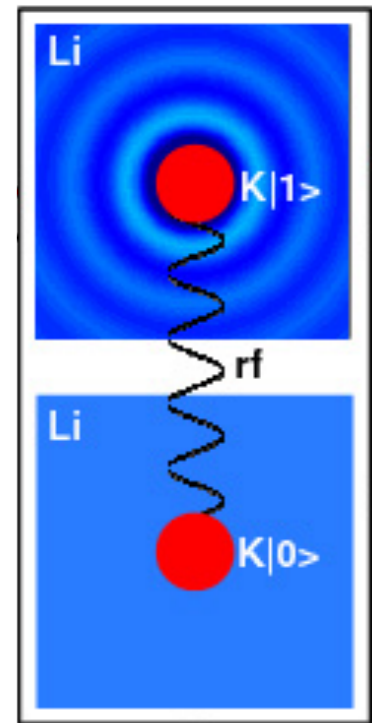
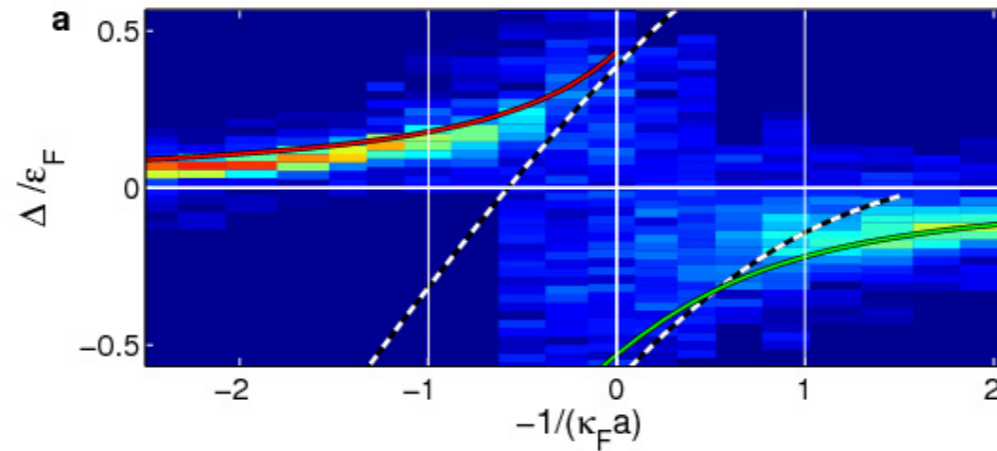
kinetic energy  
of the **polarens**

chemical potential (energy)  
of one polaron

( $m^*$  is their effective mass)

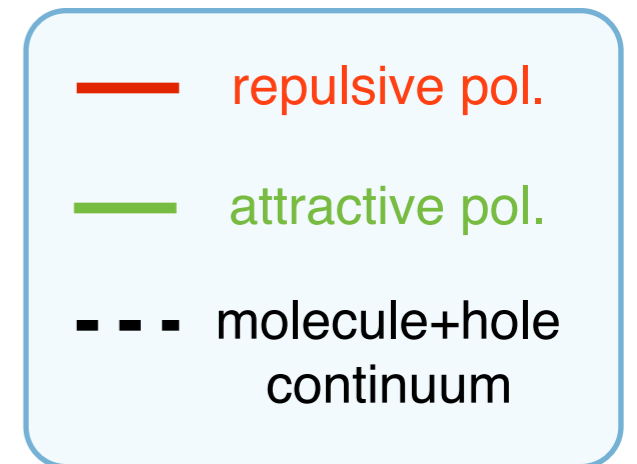
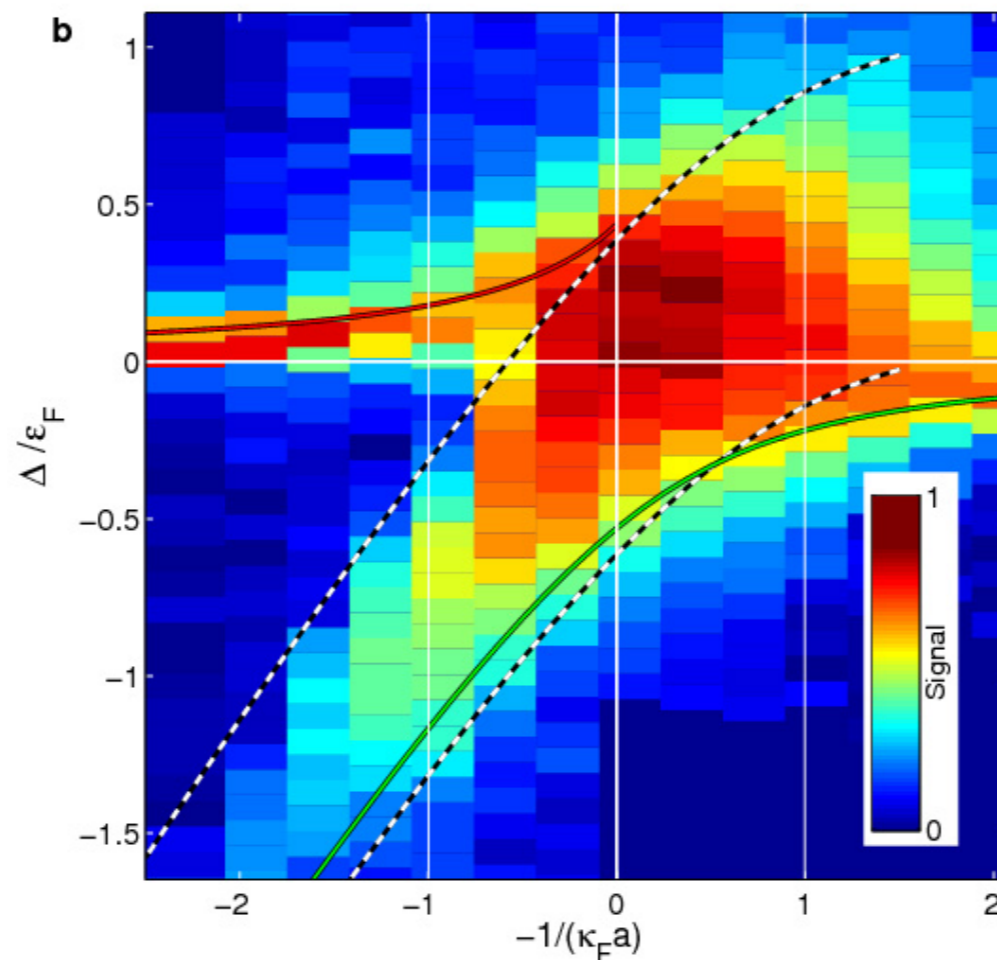
# Spectrum of Fermi polarons

low power RF:



high power RF:

high power is needed to couple to the MH continuum, due to a small FC overlap



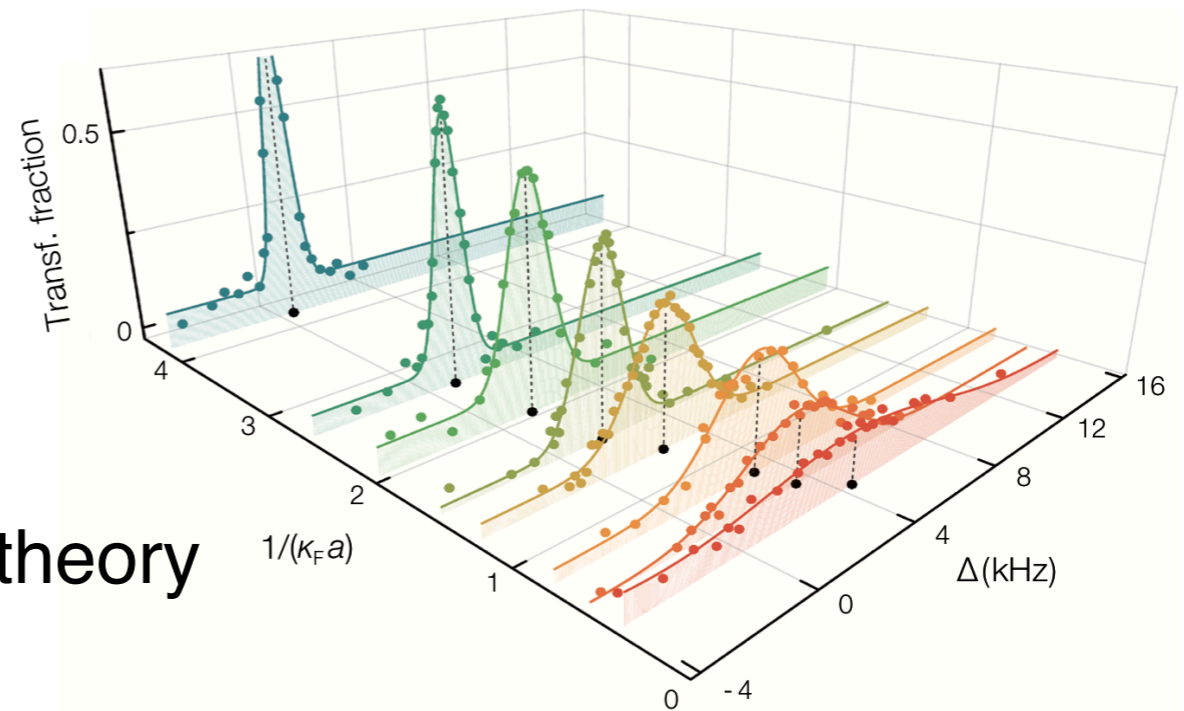
experiments: MIT (2009), ENS-Paris (2009), Innsbruck (2012), Cambridge (2012), Innsbruck (2016), LENS (2017)

theory: Chevy, Recati, Combescot, Zwirger, Enss, Schmidt, Bruun, Pethick, Zhai, Levinsen, Parish, Castin, ...

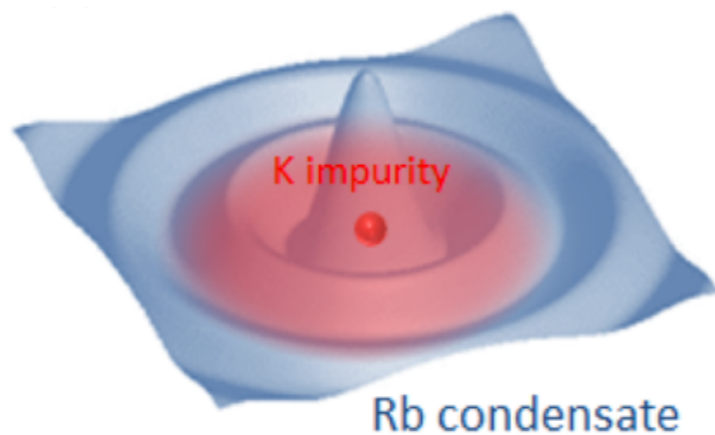
review: PM, Zaccanti and Bruun, Rep. Prog. Phys. (2014)

# Repulsive polarons

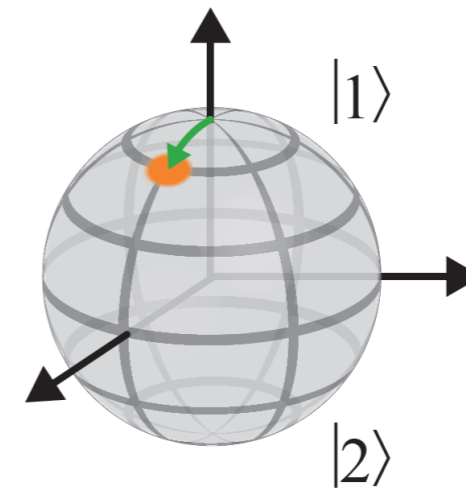
- most general case  
(equal masses, broad resonance)
- $\exists$  meta-stable quasiparticle at  $E > 0$
- long-lived, even close to unitarity
- measures of  $E$ ,  $m_{\text{eff}}$  and  $Z$   
in very good agreement with simple theory
- polaron-polaron interactions negligible



# Impurities in a Bose gas



JILA: Hu, ..., Cornell and Jin, PRL (2016)

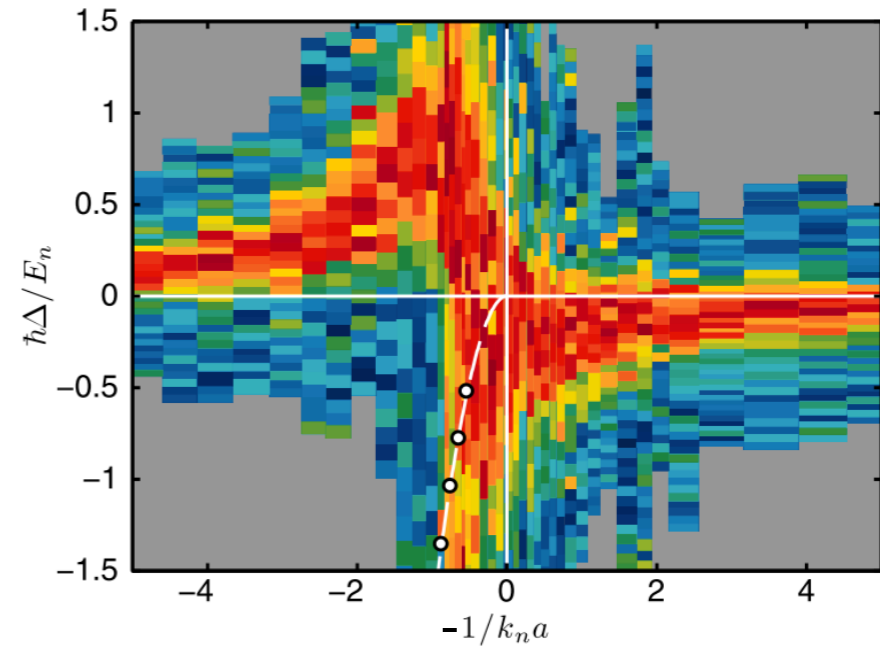
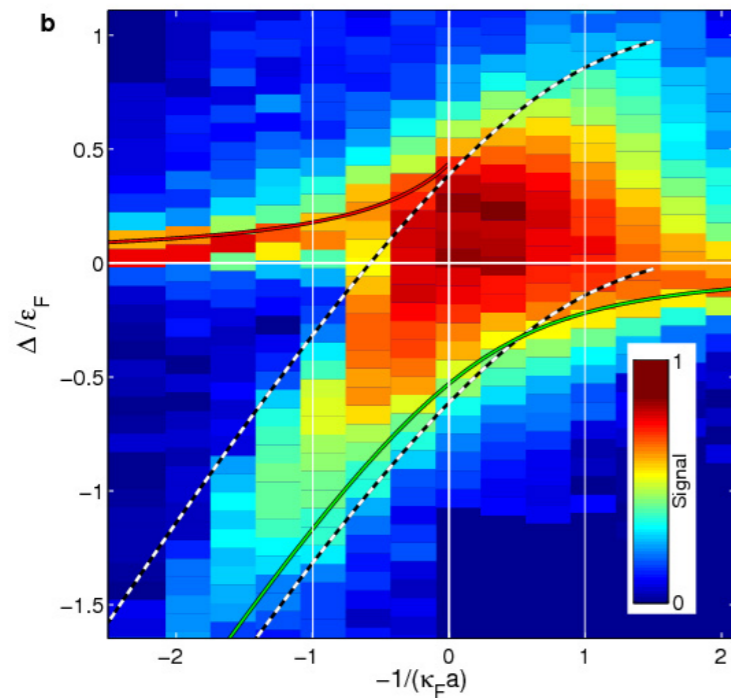


weak RF pulse + quick decoherence:  
a few  $|2\rangle$  impurities in a bath of  $|1\rangle$  atoms

Aarhus: Jørgensen, ..., Bruun and Aft, PRL (2016)

T=0 theory: Rath, Schmidt, Das Sarma, Bruun, Levinsen, Parish, Giorgini, ...

# Fermi vs. Bose



	non-interacting Fermi sea	weakly-interacting Bose gas ( $k_n a_B \ll 1$ )
Temperature	smooth crossover from degenerate to classical	BEC phase transition at $T_c$
Impurity ground state	polaron/molecule transition	smooth crossover
Three-body physics	negligible	important role
Stability	rather stable mixture	rapid three-body losses

# Definition of the problem

- Bath treated with Bogoliubov theory

» critical temperature:  $T_c = \frac{2\pi}{m_B} \left( \frac{n}{\zeta(\frac{3}{2})} \right)^{2/3} \approx 0.436 E_n$

» condensate density:  $n_0 = n[1 - (T/T_c)^{3/2}]$

» bath chemical potential:  $\mu_B = \mathcal{T}_B n_0$

» bath vacuum scattering matrix:  $\mathcal{T}_B = 4\pi a_B / m_B$

» dispersion of the excitations:  $E_{\mathbf{k}} = \sqrt{\epsilon_{\mathbf{k}}^B (\epsilon_{\mathbf{k}}^B + 2\mu_B)}$

» free bosons:  $\epsilon_{\mathbf{k}}^B = k^2 / 2m_B$

units:  $k_n = (6\pi^2 n)^{1/3}$   
 $E_n = k_n^2 / 2m_B$

- Impurity-bath coupling: **finite temperature Green's functions (non-perturbative!)**

- Polaron energy:  $\omega_{\mathbf{p}} = \epsilon_{\mathbf{p}} + \text{Re}[\Sigma(\mathbf{p}, \omega_{\mathbf{p}})]$

- Polaron residue:  $Z_{\mathbf{p}} = \frac{1}{1 - \partial_{\omega} \text{Re}[\Sigma(\mathbf{p}, \omega)]|_{\omega_{\mathbf{p}}}}$

# Diagrammatic scheme

Impurity Green's function:  $\mathcal{G}(\mathbf{p}, i\omega_j) = \frac{1}{\mathcal{G}_0(\mathbf{p}, i\omega_j)^{-1} - \Sigma(\mathbf{p}, i\omega_j)}$

$$\boxed{\mathcal{T}} = \text{wavy line} + \text{wavy line} \boxed{\mathcal{T}}$$

Ladder T-matrix:  $\mathcal{T}(\mathbf{p}, i\omega_j)^{-1} = \mathcal{T}_v^{-1} - \Pi(\mathbf{p}, i\omega_j)$

- - - BEC boson
- excited boson
- impurity

T>0: important diagram missing in ladder approx:



$$\Sigma = \underbrace{\boxed{\mathcal{T}} + \boxed{\mathcal{T}}}_{\Sigma_L}$$

T=0 ladder: Rath and Schmidt, PRA 2013

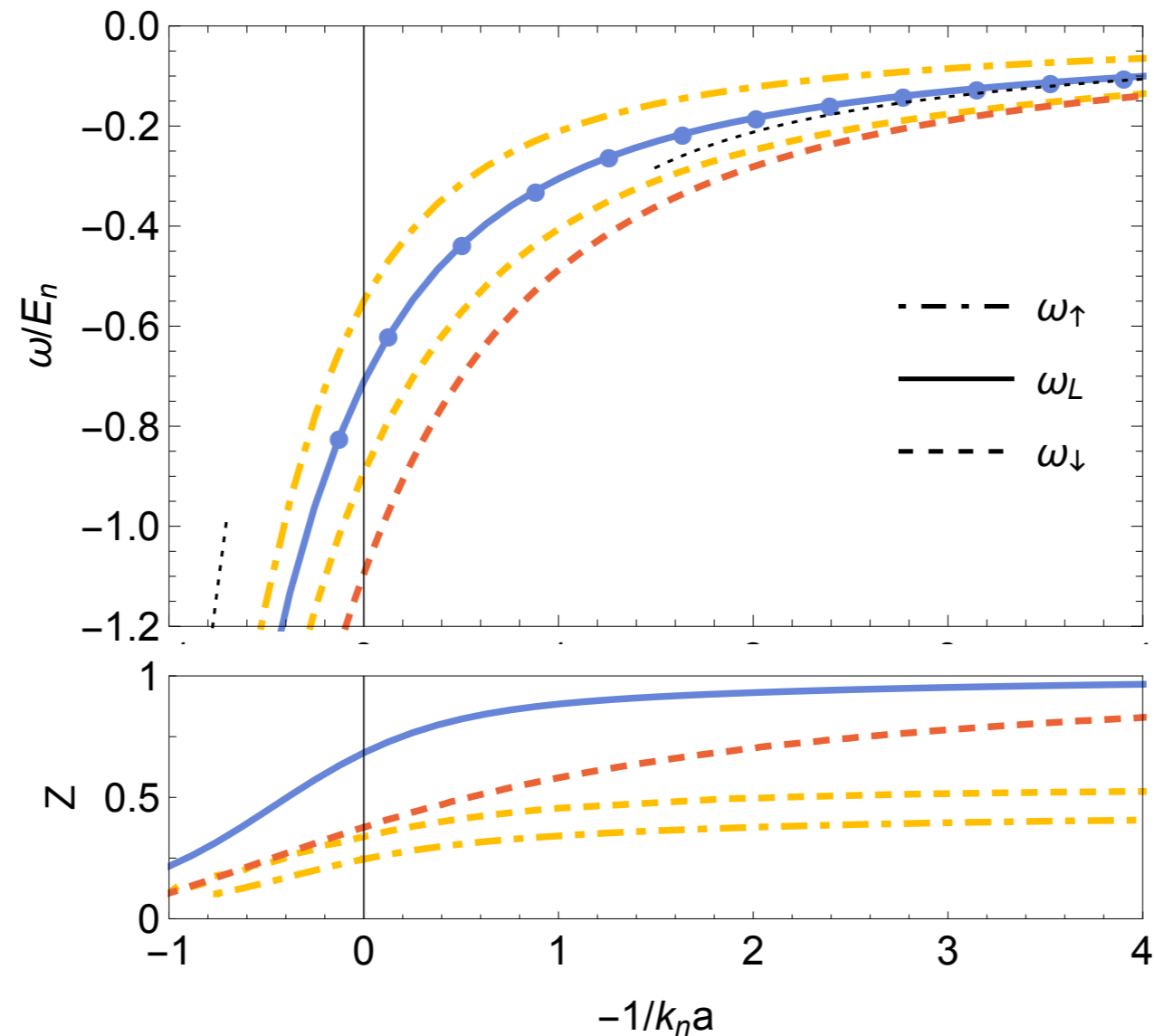
Perturbation theory at T>0: Levinsen, Parish, Christensen, Arlt, and Bruun, arXiv:1708.09172

Extended T>0 diagrammatic scheme: Guenther, PM, Lewenstein and Bruun, arXiv:1708.08861

# Varying coupling strength

Aarhus:  $k_n a_B = 0.01$

$T=0$   
 $T=0.5T_c$   
 $T=T_c$



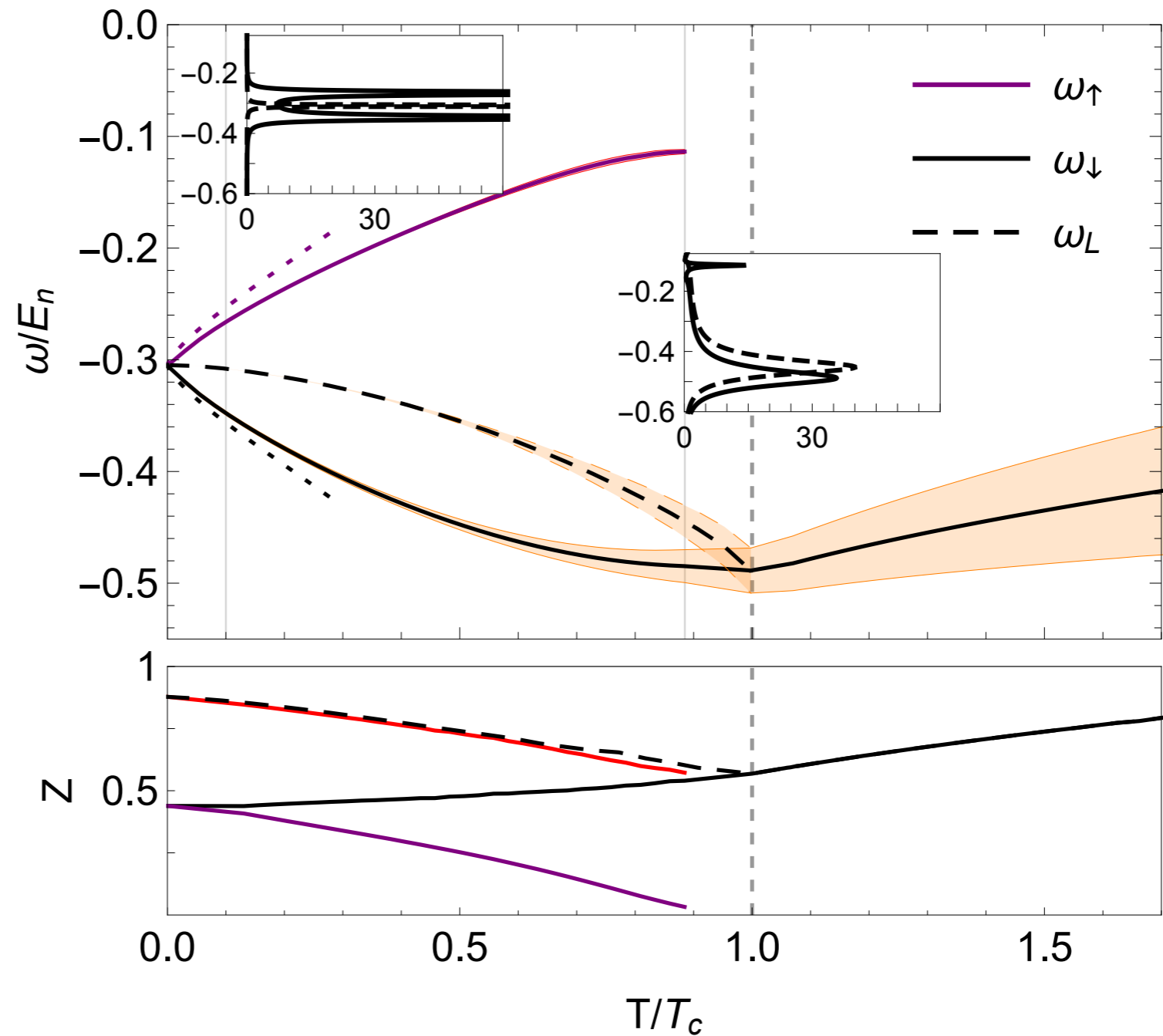
dots:  $T=0$  ladder theory by  
Rath and Schmidt, PRA 2013



# Varying temperature

Weak attraction  
( $k_n a = -1$ )

Energy:

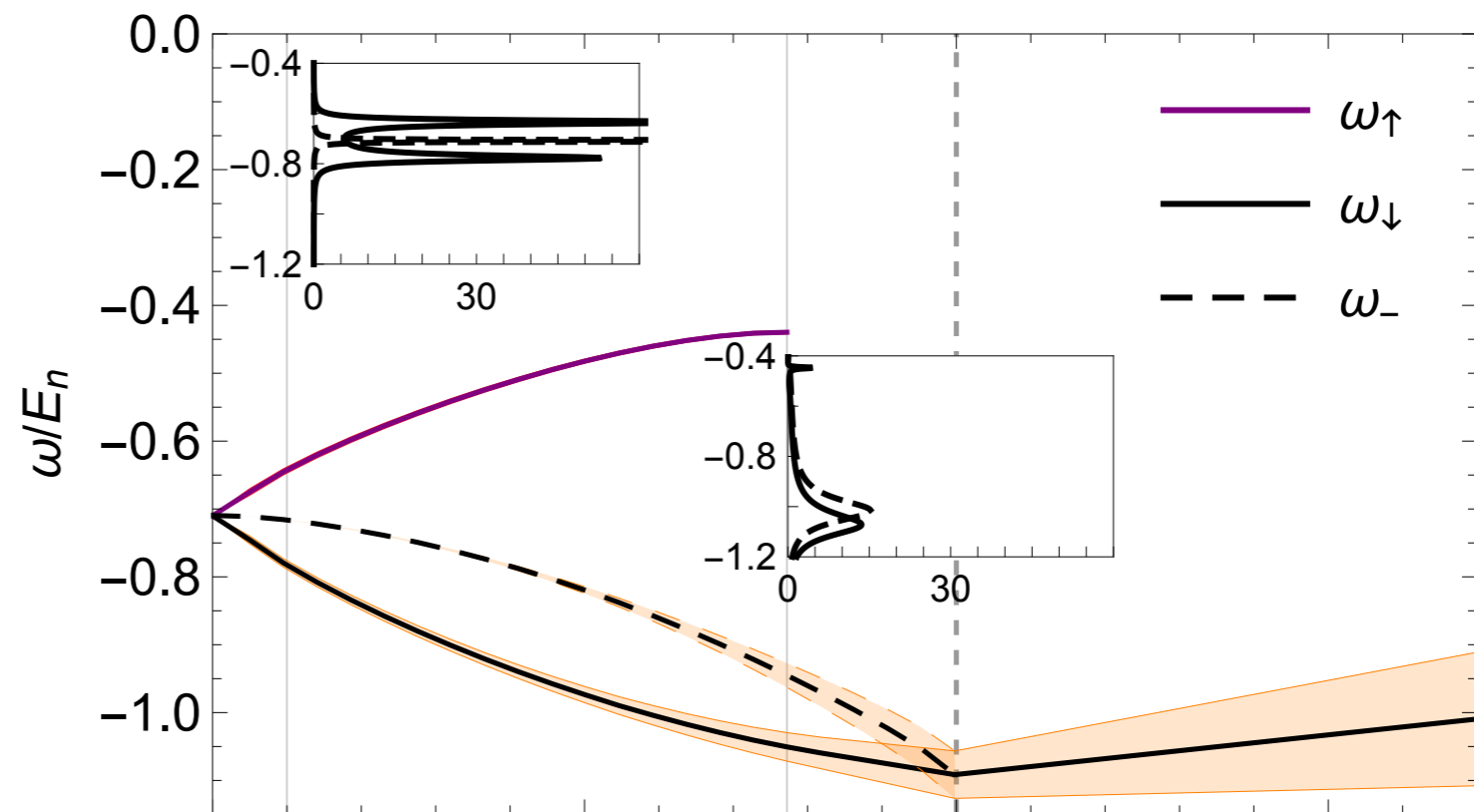


Residue:

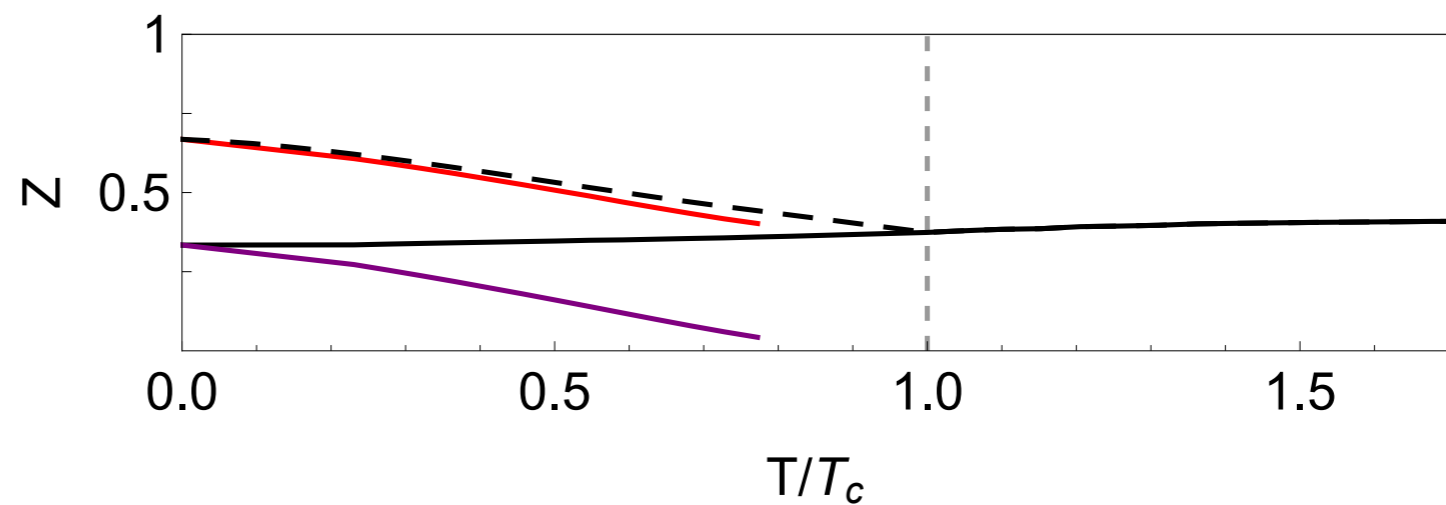
# Varying temperature

Strong attraction  
(unitarity)

Energy:



Residue:



# Understanding fragmentation

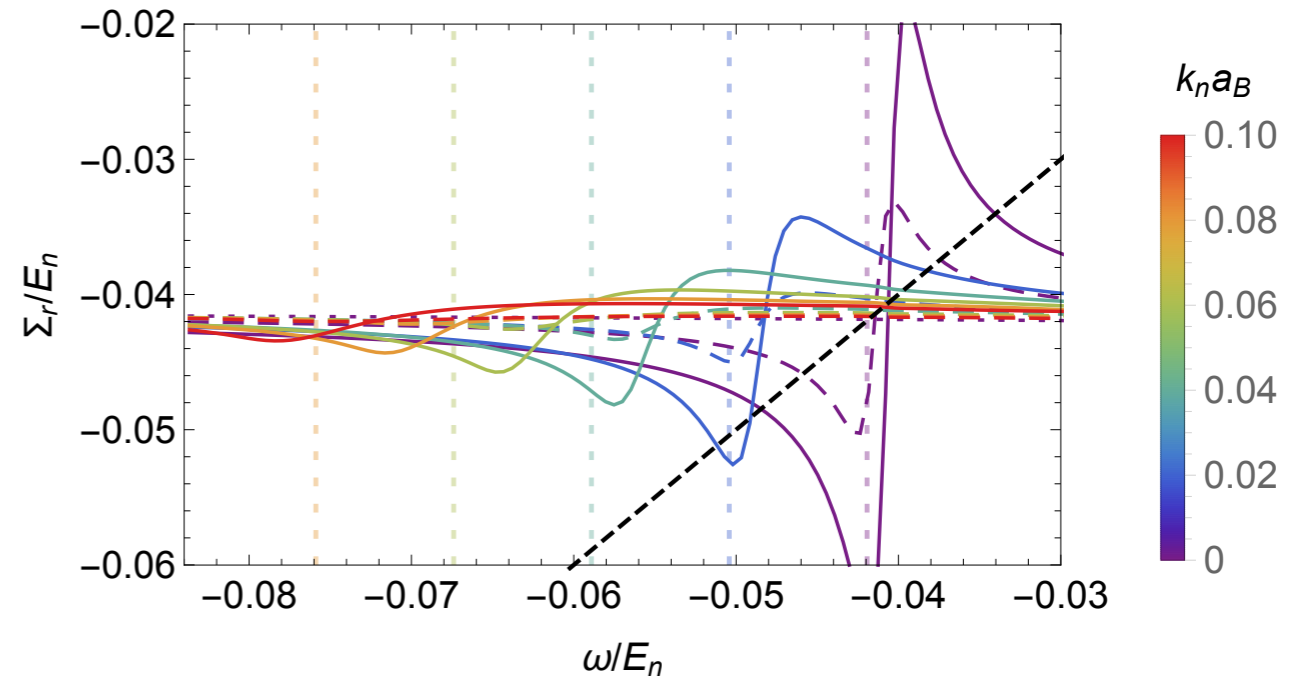
$$\omega_0 = \text{Re}[\Sigma(\mathbf{p} = 0, \omega_0)]$$

Weak coupling,

low temperature behavior of  $\text{Re}(\Sigma)$ :

$$(k_n a = -0.1)$$

dashed:  $T = 0.05T_c$   
solid:  $T = 0.1T_c$



$$\Sigma_1(\omega) \approx \int \frac{d^3 k}{(2\pi)^3} \frac{f_{\mathbf{k}}}{\mathcal{T}_v^{-1} - \Pi(\mathbf{k}, \omega + E_{\mathbf{k}}) - \frac{n_0}{\omega + E_{\mathbf{k}} - \epsilon_{\mathbf{k}}}}$$

← on-shell for:  $\omega + E_{\mathbf{k}} = \epsilon_{\mathbf{k}} + \Sigma_0(\mathbf{k}, \omega + E_{\mathbf{k}})$

$$\approx \frac{\omega + n_0 \mathcal{T}_B}{\omega - n_0 (\mathcal{T}_v - \mathcal{T}_B)} n_{\text{ex}} \mathcal{T}_v$$

non-condensed fraction

$|a| \gtrsim a_B$  : equal splitting

$$\omega_{\uparrow, \downarrow} \simeq \omega_0 [1 \pm (Z_0 n_{\text{ex}} / n_0)^{1/2}]$$

$$Z_{\uparrow, \downarrow} \simeq Z_L / 2$$

$|a| \lesssim a_B$  : single polaron

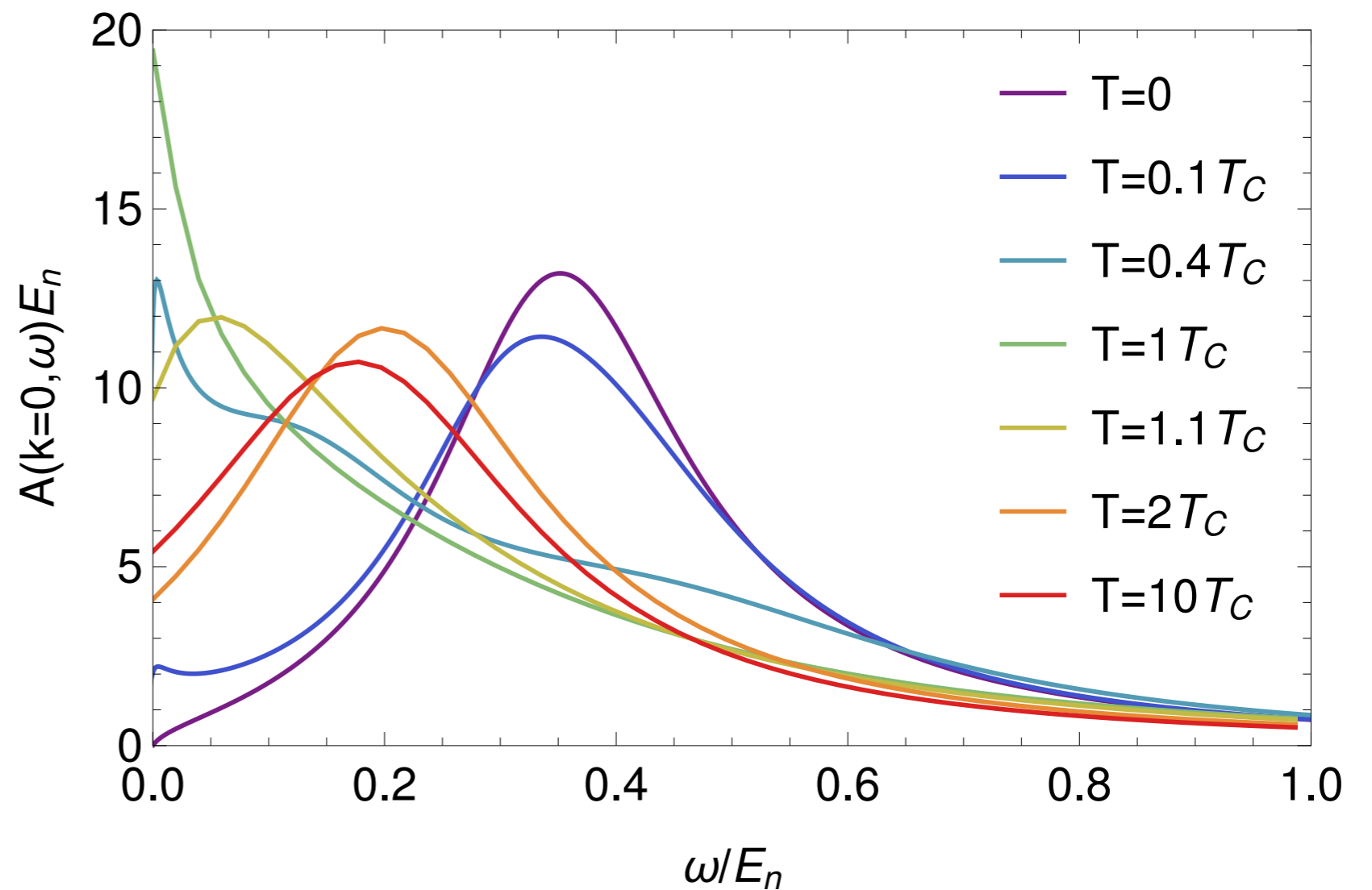
$$\omega_{\uparrow} \simeq n \mathcal{T}_v$$

in accord with perturbation theory [Levinsen et al., arXiv:1708.09172]

# Repulsive polarons

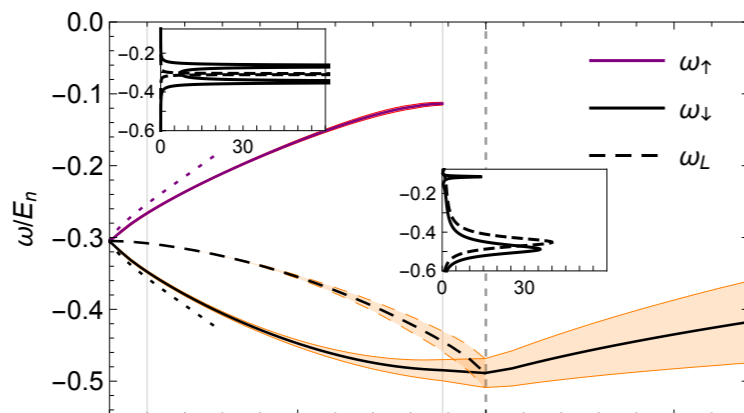
Weak repulsion  
( $k_n a = 1$ )

Spectral function:



# Conclusions

- Bose polarons greatly differ from Fermi ones
- No polaron/molecule transition
- Fundamental role played by the BEC, and the associated large low-energy density of states
- Non-perturbative treatment is crucial
- The  $T=0$  attractive polaron fragments into two quasiparticles at  $T>0$
- The upper of the two negative energy excitations disappears at  $T_c$
- The ground state quasiparticle remains well-defined across  $T_c$



**Thank you!**